

EFFECT OF PITCH PROGRAM
VARIATIONS ON LAUNCH AVAILABILITY
OF ATLAS/CENTAUR-AC-7 TO AC-15
(PHASE I)

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FOREWORD

This report, GD/A-DDE64-045, documents Phase I of a study to improve the Launch Availabilty of the Atlas/Centaur series AC-7 through AC-15. It documents the rules of analysis, presents data on launch capability, and indicates the course of action for further analysis, as well as presenting the benefits to be gained by improving pitch programs, increasing tank pressure, and reducing gust velocity criterion.

SUMMARY

Six initial pitch programs were generated by iterating the Atlas/Centaur trajectories to simultaneously meet payload, thermodynamic, aerodynamic, and inertia load constraints for launch during any season of the year. Each pitch program was selected to produce approximately zero angle-of-attack through one of six average wind profiles. Basic assumptions included a gust velocity criterion of 40 ft/sec., a factor of safety on bending moment and axial load of 1.25, 165,000 lb. thrust on each booster engine, Atlas LO₂ tank pressure of 28.5 psig after 20 seconds of flight and Centaur LH₂ tank pressure of 19.5 psia at liftoff. Using the above assumptions with six pitch programs and performing trajectory simulations on the IBM 7090 for real wind data, Tables 1-7 through 1-12 were obtained. From these tables, Figure 1-2 was constructed. It may be observed from Figure 1-2 that only three pitch programs are needed throughout the year. Use of the best three pitch programs produced a percent launch availability of 100 percent in July, 90 percent in August, 64 percent in June and September, 50 percent in May and October, 40 percent in January, November, and April, and 10 percent in February, March and December.

Since completion of this work, however, data has been obtained on the AC-5 configuration with a factor of safety on the axial load of 1.10, a gust velocity criterion of 30 ft/sec., an improved pitch program, and increased tank pressures based upon statistical telemetered data and quad tanking data. The minimum launch availability with this data has been tentatively increased to 50 percent and will be documented in the next report on this subject.

The work contained herein considers the benefit to the launch availability by increasing the Atlas LO₂ tank minimum pressure from 28.5 psig to 33.5 psig at 20 seconds of flight and by increasing the Centaur LH₂ tank minimum pressure from 19.5 psia to 22.0 psia at liftoff. This amount of pressure increase can increase the percent launch availability by as much as 20 percent, as shown in Figure 2-2. Also considered is a reduction in the gust velocity criterion from 40 ft/sec. to 30 ft/sec., which produces a launch availability increase of 23 percent in the worst winter months, as shown in Figure 2-4. Modifications of the initial pitch programs used in this study are expected to increase the launch availability because the biasing is based on real wind profiles instead of average profiles. Not considered in this report is the use of an axial load factor of safety of 1.10 instead of 1.25. The reduced factor of safety increases the launch availability by 8 to 10 percent.

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EFFECTS OF PITCH PROGRAM VARIATIONS
ON LAUNCH AVAILABILITY OF ATLAS/CENTAUR
AC-7 TO AC-15
(PHASE I)

SECTION I

INTRODUCTION

1.1 OBJECTIVE

The purpose of this document is to investigate possible methods to improve launch capability of the Atlas/Centaur vehicle beginning with the AC-7 configuration, as defined in Reference 1, and continuing on through to the AC-15 configuration.

Accomplishment of this task can be achieved by improving the current three best pitch programs, increasing pressure in the Atlas and Centaur tanks, and reducing the gust velocity criterion.¹

Note¹

For this study (1-cosine) gust with a maximum gust velocity of 40 ft/sec is being used. Since the wind profiles are derived from balloon data which is taken every 1000 ft. the gust velocity criteria is to approximate the short wave length phenomena and include the effects of transonic buffet, errors in balloon and radar measurements, and the lack of persistence of the wind profile between the time of observation and the time of flight. This report shows the effect of reducing the gust velocity criterion, and not the justification which is subject to consideration.

This section offers data on wind profiles, pitch programs, and existing percent launch availability information. Later sections detail, along with graphs, mathematical equations, and tables, the suggested methods for improving launch capability, pitch programs, and yaw programs.

1.2 WIND PROFILES AND PITCH PROGRAMS

The starting point for this study was to select from the set of AMR mean monthly wind profiles, documented in Reference 2, a reduced set which would be representative of the mean variation throughout the year. The intent was to generate a series of pitch programs which would cover the entire year with a nearly optimum launch availability.

It was observed that certain months of the year had mean wind profiles similar to other months. These were consequently grouped and approximated by a single wind function. A total of six wind profiles (WP) were constructed and labeled (130, 100, 70, 30, 0, -20) corresponding to the value of the wind velocity of each profile at an altitude of 40,000 feet. The AMR mean monthly profiles and the constructed set of six functions are shown in Figure 1-1. These are representative of the spectrum of monthly variations.

1.2.1 PITCH PROGRAM. Corresponding to each of the six Wind Profiles (WP), a set of six Pitch Programs (PP) were developed which maintained the vehicle at approximately zero angle-of-attack through the region of maximum dynamic pressure and then to booster engine cutoff (BECO). The pitch programs are stepped functions which conform to the input requirements of the Atlas autopilot.

The pitch programs and months they pertain to are as follows:

- | | |
|--------------|---------|
| a. February | |
| March | PP130 |
| December | |
| b. January | |
| November | PP100 |
| April | |
| c. May | PP70 |
| October | |
| d. September | PP30 |
| June | |
| e. August | PP0 |
| f. July | PP(-20) |

Pitch programs are defined by their pitch rates or the rate at which the vehicle is pitching over as the altitude increases. The pitch rates are summarized in Tables 1-1 to 1-6 for the six pitch programs mentioned previously.

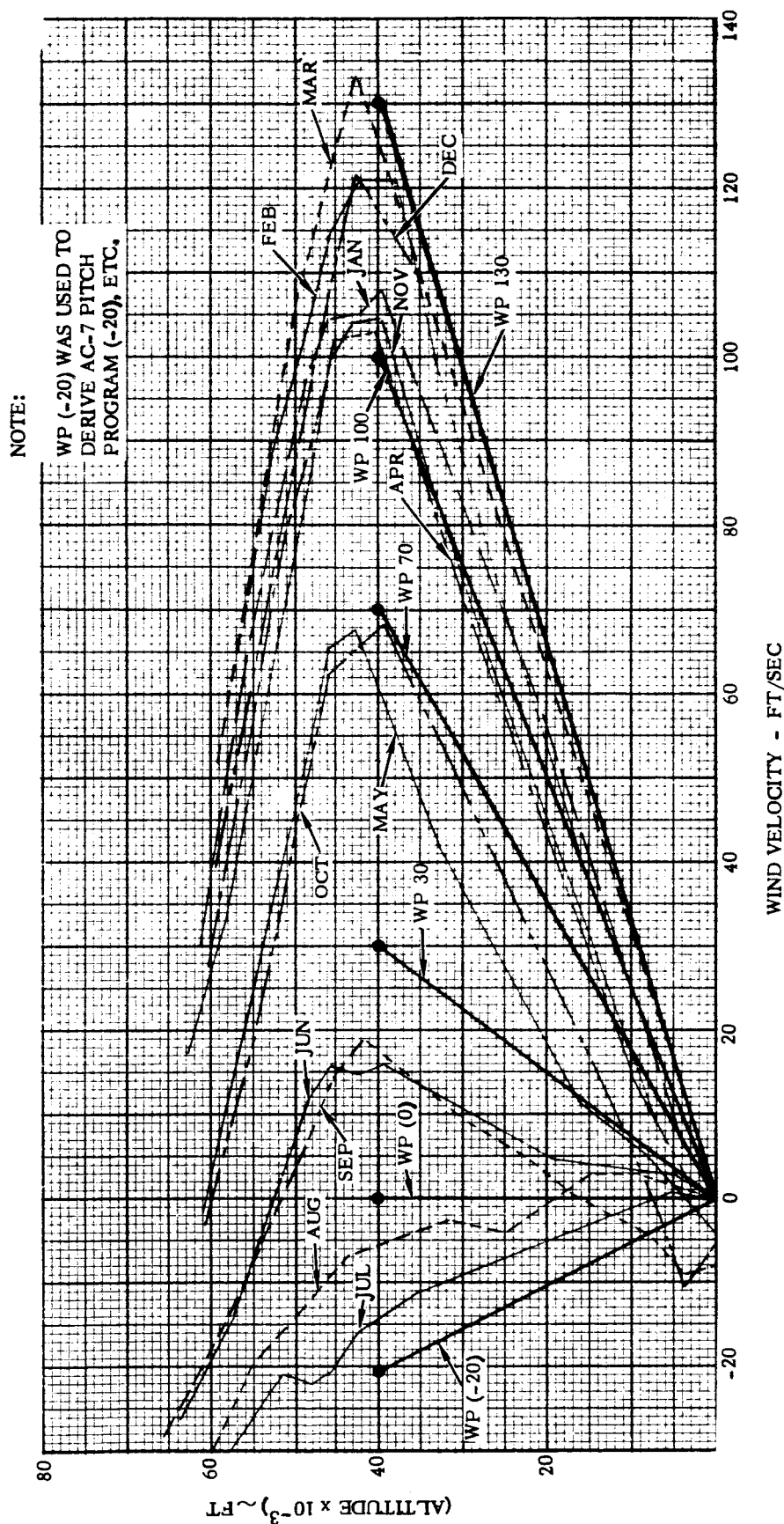


Figure 1-1. AMR Monthly Mean Wind Profiles

2W01ST

TABLE 1-1. PITCH RATES FOR
PITCH PROGRAM
(130)

| Time In Flight (seconds) | Pitch Rate (degrees/second) |
|--------------------------------|--------------------------------|
| 0-15 | .00 |
| 15-64 | .6375 |
| 64-72 | .5865 |
| 72-82 | .7650 |
| 82-90 | .6650 |
| 90-96 | .5865 |
| 96-102 | .4335 |
| 102-114 | .3570 |
| 114-128 | .3060 |
| 128-160 | .2295 |

TABLE 1-2. PITCH RATES FOR
PITCH PROGRAM
(100)

| Time In Flight (seconds) | Pitch Rate (degrees/second) |
|--------------------------------|--------------------------------|
| 0-15 | .00 |
| 15-46 | .6120 |
| 46-62 | .6885 |
| 62-74 | .6375 |
| 74-80 | .7905 |
| 80-90 | .6630 |
| 90-98 | .5610 |
| 98-112 | .3825 |
| 112-128 | .3060 |
| 128-160 | .2295 |

TABLE 1-3. PITCH RATES FOR
PITCH PROGRAM
(70)

| Time In Flight (seconds) | Pitch Rate (degrees/second) |
|--------------------------------|--------------------------------|
| 0-15 | .00 |
| 15-42 | .575 |
| 42-58 | .700 |
| 58-74 | .650 |
| 74-82 | .750 |
| 82-90 | .650 |
| 90-98 | .550 |
| 98-112 | .400 |
| 112-122 | .325 |
| 122-160 | .250 |

TABLE 1-4. PITCH RATES FOR
PITCH PROGRAM
(30)

| Time In Flight (seconds) | Pitch Rate (degrees/second) |
|--------------------------------|--------------------------------|
| 0-15 | .00 |
| 15-38 | .5271 |
| 38-48 | .7028 |
| 48-58 | .7530 |
| 58-84 | .7028 |
| 84-94 | .6024 |
| 94-108 | .4518 |
| 108-126 | .3263 |
| 126-160 | .2259 |

TABLE 1-5. PITCH RATES FOR
PITCH PROGRAM
(0)

| Time In Flight (seconds) | Pitch Rate (degrees/second) |
|--------------------------------|--------------------------------|
| 0-15 | .00 |
| 15-34 | .4769 |
| 34-44 | .6777 |
| 44-64 | .7530 |
| 64-80 | .7028 |
| 80-88 | .6526 |
| 88-96 | .5522 |
| 96-104 | .4769 |
| 104-118 | .3765 |
| 118-160 | .2510 |

TABLE 1-6. PITCH RATES FOR
PITCH PROGRAM
(-20)

| Time In Flight (seconds) | Pitch Rate (degrees/second) |
|--------------------------------|--------------------------------|
| 0-15 | .00 |
| 15-32 | .4369 |
| 32-46 | .6939 |
| 46-64 | .7710 |
| 64-82 | .7196 |
| 82-92 | .5911 |
| 92-104 | .4883 |
| 104-116 | .3855 |
| 116-126 | .3084 |
| 126-150 | .2313 |

Thirty winds were run for the month in which the pitch program was designed, and in the months for which the pitch program was not designed, it was assumed that 10 runs would be sufficient. This makes a total of 80 runs per pitch program.

1.3 PRESENT PERCENT LAUNCH AVAILABILITY

To find the present percent launch availability, Stations 219, 410, 568, and 770 were checked by use of the SC 4020 plots of the IBM 7090 trajectory solutions to determine if the design limit bending moments were exceeded and the engine deflection in the pitch plane was also checked, utilizing data from Reference 3, to determine if it had exceeded its allowable value. The results are shown in Table 1-7 through Table 1-12.

1.3.1 MONTHLY PITCH PROGRAM EVALUATION. To calculate the percent launch availability, the number of runs in which the values of bending moment and engine deflection had not exceeded the allowable design limit was divided by the total number of runs, and then multiplied by one hundred. Figure 1-2 plots the percent launch availability versus months for all the pitch programs.

TABLE 1-7. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 130 AND $V_g = 40$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δp | | Date | Bending Moment At Station | | | | Eng. Def. δp | |
|-----------------------------------|---------|------------------------------|-----|-----|-----|--------------------|-----------------------------------|---------|------------------------------|-----|-----|-----|--------------------|--|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | | |
| JAN NOV APR L.A.=40% | 1955 10 | | X | | X | | SEPT JUNE L.A.=10% | 1958 11 | | | | X | X | |
| | 1955 15 | X | X | | X | | | 1958 16 | | X | | | X | |
| | 1956 12 | X | X | X | X | X | | 1959 6 | | X | | X | X | |
| | 1957 12 | | | | | | | 1960 11 | X | X | | X | X | |
| | 1957 19 | | | | | | | 1960 16 | | X | | X | X | |
| | 1958 12 | X | X | X | X | X | | 1961 11 | X | X | X | X | X | |
| | 1958 15 | X | X | X | X | X | | 1961 16 | | X | | X | X | |
| | 1959 12 | | | | | | | 1962 11 | X | X | X | X | X | |
| 1959 15 | X | X | X | X | X | 1962 16 | X | X | X | X | X | | | |
| MAY OCT L.A.=40% | 1958 11 | | | | | | FEB MAR DEC L.A.=10% | 1955 2 | | | | | | |
| | 1958 16 | | | | | | | 1955 5 | X | X | X | X | X | |
| | 1959 11 | | X | | | | | 1955 11 | X | X | X | X | | |
| | 1960 11 | X | X | X | X | | | 1955 17 | X | X | X | X | X | |
| | 1960 16 | | | | | | | 1955 23 | | X | | X | | |
| | 1961 11 | X | X | X | X | X | | 1955 26 | | X | | X | | |
| | 1961 16 | | X | | | | | 1956 2 | | | | X | | |
| | 1962 11 | | X | | X | | | 1956 5 | X | X | X | X | | |
| JULY L.A.=0% | 1958 11 | | X | | X | X | | 1956 11 | X | X | X | X | X | |
| | 1958 16 | | X | | X | X | | 1956 14 | | X | | X | | |
| | 1959 11 | | X | | X | X | | 1956 17 | | | | X | | |
| | 1960 11 | X | X | X | X | X | | 1956 23 | | | | X | | |
| | 1960 16 | | | | | | | 1957 2 | | X | | | | |
| | 1961 11 | X | X | X | X | X | | 1957 5 | | | | | | |
| | 1961 16 | | X | | X | X | | 1957 11 | | X | | X | X | |
| | 1962 11 | X | X | X | X | X | | 1957 17 | X | X | X | X | X | |
| AUG L.A.=20% | 1958 11 | | X | | X | X | | 1957 20 | X | X | X | X | X | |
| | 1958 16 | | X | | | | | 1957 26 | X | X | X | X | X | |
| | 1959 11 | | X | | | | | 1958 2 | X | X | X | X | X | |
| | 1960 11 | X | X | X | X | X | | 1958 5 | X | X | X | X | X | |
| | 1960 16 | | | | | | | 1958 11 | X | X | X | X | X | |
| | 1961 11 | X | X | X | X | X | | 1958 17 | X | X | X | X | X | |
| | 1961 16 | | | | | | | 1958 20 | X | X | X | X | X | |
| | 1962 11 | X | X | X | X | X | | 1958 25 | X | X | X | X | X | |
| 1962 16 | | X | X | X | | | | | | | | | | |
| X: Exceeds Allowable | | | | | | | | | | | | | | |

TABLE 1-8. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 100 AND $V_g = 40$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δp | | Date | Bending Moment At Station | | | | Eng. Def. δp |
|----------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|-----------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| FEB MAR DEC L.A.=0% | 1955 11 | X | X | X | X | | SEPT JUNE L.A.=50% | 1958 11 | | | | | |
| | 17 | X | X | X | X | X | | 16 | | | | | |
| | 1956 11 | X | X | X | X | X | | 1959 11 | | | | | |
| | 17 | | | | X | | | 21 | | | | | |
| | 1957 11 | | X | X | X | | | 1960 11 | X | X | | X | X |
| | 17 | X | X | X | X | | | 16 | | | | | |
| | 1958 11 | X | X | X | X | | | 1961 11 | X | X | X | X | |
| | 17 | X | X | X | X | X | | 16 | | | | | X |
| MAY OCT L.A.=50% | 1959 11 | X | X | X | X | | JAN NOV APR L.A.=20% | 1962 11 | | X | | X | X |
| | 17 | X | X | X | X | X | | 16 | X | X | X | X | X |
| | 1958 11 | | | | | | | 1955 3 | | | | | |
| | 16 | | | | | | | 6 | | X | | | X |
| | 1959 11 | | | | | | | 10 | | X | | X | |
| | 16 | | | | X | | | 15 | | X | | | |
| | 1960 11 | X | X | X | X | | | 21 | X | X | X | X | X |
| | 16 | | | | | | | 27 | X | X | X | X | X |
| JULY L.A.=40% | 1961 11 | X | X | X | X | X | | 1956 3 | | X | | X | |
| | 16 | | | | | | | 6 | | | | | |
| | 1962 11 | | X | | X | | | 12 | X | X | X | X | |
| | 16 | | X | | | | | 15 | | | | | |
| | 1958 11 | | | | | | | 21 | X | X | X | X | X |
| | 16 | | | | | | | 27 | | X | | X | |
| | 1959 11 | | X | | X | X | | 1957 3 | | X | | X | X |
| | 16 | | | | | | | 6 | X | X | X | X | X |
| AUG L.A.=80% | 1960 11 | | X | | X | X | | 12 | | | | | |
| | 16 | | | | | | | 19 | | | | X | |
| | 1961 11 | | X | | X | X | | 21 | | X | | X | |
| | 16 | | X | | | X | | 27 | | | | | |
| | 1962 11 | | X | | X | X | | 1958 3 | X | X | X | X | X |
| | 16 | | X | X | X | X | | 6 | X | X | X | X | X |
| | 1958 11 | | X | | | | | 12 | X | X | X | X | X |
| | 16 | | | | | | | 15 | X | X | X | X | X |
| | 1959 11 | | | | | | | 21 | X | X | X | X | X |
| | 16 | | | | | | | 27 | X | X | X | X | X |
| | 1960 11 | X | | | X | X | | 1959 3 | | X | | X | |
| | 16 | | | | | | | 6 | X | X | X | X | |
| | 1961 11 | | | | | | | 12 | | | | | |
| | 16 | | | | | | | 15 | X | X | X | X | X |
| | 1962 11 | | | | | | | 21 | | X | | | |
| | 16 | | | | | | | 27 | | X | | X | |

X: Exceeds Allowable

TABLE 1-9. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 70 AND $V_g = 40$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δp | | Date | Bending Moment At Station | | | | Eng. Def. δp |
|-----------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| JAN NOV APR L.A.=30% | 1955 10 | | X | | X | | AUG L.A.=90% | 1958 11 | | | | | |
| | 1955 15 | | X | | X | | | 1958 16 | | | | | |
| | 1956 12 | X | X | X | X | X | | 1959 11 | | | | | |
| | 1957 12 | | | | | | | 1960 11 | | X | | X | X |
| | 1957 19 | | X | | X | | | 1960 16 | | | | | |
| | 1958 12 | X | X | X | X | X | | 1961 11 | | | | | |
| | 1958 15 | X | X | X | X | X | | 1961 16 | | | | | |
| FEB MAR DEC L.A.= 0% | 1959 12 | | | | | | MAY OCT L.A.=43.3% | 1962 11 | | | | | |
| | 1959 15 | X | X | X | X | X | | 1962 16 | | | | | |
| | 1955 11 | X | X | X | X | X | | 1958 1 | | | | X | |
| | 1955 17 | X | X | X | X | X | | 1958 6 | | | | | |
| | 1956 11 | | | | | | | 1958 11 | | | | | |
| | 1957 11 | | X | | | | | 1958 16 | | | | | |
| | 1957 17 | | X | X | X | X | | 1959 1 | | X | X | X | |
| JULY L.A.= 50% | 1958 11 | X | X | X | X | X | | 1959 6 | X | X | X | X | X |
| | 1958 17 | X | X | X | X | X | | 1959 11 | | | | | |
| | 1958 11 | X | X | X | X | X | | 1959 16 | | X | | X | |
| | 1959 11 | X | X | X | X | X | | 1960 1 | | X | | | |
| | 1959 17 | X | X | X | X | X | | 1960 6 | | X | X | X | X |
| | 1959 11 | X | X | X | X | X | | 1960 11 | X | X | X | X | X |
| | 1959 17 | X | X | X | X | X | | 1960 16 | | | | | |
| SEPT JUNE L.A.=60% | 1958 11 | | | | | | | 1960 21 | | X | | X | X |
| | 1958 16 | | | | | | | 1960 26 | X | X | X | X | X |
| | 1959 11 | | | | | | | 1961 1 | | X | X | X | X |
| | 1959 16 | | | | | | | 1961 6 | | | | | |
| | 1960 11 | X | | X | X | X | | 1961 11 | X | X | X | X | X |
| | 1960 16 | | | | | | | 1961 16 | | X | X | X | X |
| | 1961 11 | X | X | X | X | | | 1961 21 | | X | | X | |
| | 1961 16 | | | | | | | 1961 26 | | | | | |
| | 1962 11 | | X | | X | X | | 1962 1 | X | X | X | X | X |
| | 1962 16 | | X | | X | X | | 1962 6 | | X | X | X | X |
| | | | | | | | | 1962 11 | | X | | X | |
| | | | | | | | | 1962 16 | | X | | X | |
| | | | | | | | | 1962 21 | | | | | |
| | | | | | | | | 1962 26 | | | | | |

X: Exceeds Allowable

TABLE 1-10. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 30 AND $V_g = 40$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δ_p | | Date | Bending Moment At Station | | | | Eng. Def. δ_p |
|-----------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| JAN NOV APR L.A.=20% | 1955 10 | X | X | X | X | | AUG L.A.=90% | 1958 11 | | | | | |
| | 15 | | X | | X | | | 16 | | | | | |
| | 1956 12 | X | X | X | X | X | | 1959 11 | | | | | |
| | 15 | | | | | | | 16 | | | | | |
| | 1957 12 | | X | | X | | | 1960 11 | | X | | | |
| | 19 | | X | | X | | | 16 | | | | | |
| | 1958 12 | X | X | X | X | X | | 1961 11 | | | | | |
| FEB MAR DEC L.A.=0% | 15 | X | X | X | X | X | SEPT JUNE L.A.=63% | 1962 11 | | | | | |
| | 1959 12 | X | X | X | X | X | | 16 | | | | | |
| | 15 | X | X | X | X | X | | 1958 1 | | | | | |
| | 1955 11 | X | X | X | X | | | 6 | | X | | X | |
| | 17 | X | X | X | X | | | 11 | | | | | |
| | 1956 14 | | X | X | X | | | 16 | | | | | |
| | 17 | | X | | X | | | 21 | | | | X | |
| MAY OCT L.A.=30% | 1957 14 | X | X | X | X | | | 26 | | | | | |
| | 17 | X | X | X | X | X | | 1959 1 | | | | | |
| | 1958 11 | X | X | X | X | X | | 6 | | | | | |
| | 17 | X | X | X | X | X | | 11 | | | | | |
| | 1959 14 | | X | | X | | | 16 | | X | | | |
| | 17 | X | X | X | X | X | | 21 | | X | | X | |
| | | | | | | | | 26 | | | | | |
| JULY L.A.=100% | 1958 11 | | | | | | | 1960 1 | | | | | |
| | 16 | | | | | | | 6 | | | | | |
| | 1959 11 | | X | | X | X | | 11 | | X | | X | |
| | 16 | | | | | | | 16 | | | | | |
| | 1960 11 | X | X | X | X | X | | 21 | X | X | X | X | X |
| | 16 | | | | | | | 26 | | | | | |
| | 1961 11 | X | X | X | X | | | 1961 1 | | | | | |
| | 16 | | | | | | | 6 | | X | X | X | X |
| | 1962 11 | X | X | X | X | | | 11 | X | X | X | X | X |
| | 16 | | X | X | X | | | 16 | | | | | |
| | | | | | | | | 21 | | | | | |
| | 1958 11 | | | | | | | 26 | | | | | |
| | 16 | | | | | | | 1962 1 | | | | | |
| | 1959 11 | | | | | | | 6 | | | | | |
| | 16 | | | | | | | 11 | | | | | |
| | 1960 11 | | | | | | | 16 | | | | | |
| | 16 | | | | | | | 21 | | | | | |
| | 1961 11 | | | | | | | 26 | | | | | |
| | 16 | | | | | | | 1962 1 | | | | | |
| | 1962 11 | | | | | | | 6 | | | | | |
| | 16 | | | | | | | 11 | | | | | |
| | | | | | | | | 16 | | | | | |
| | 1958 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |
| | 1959 11 | | | | | | | 1962 1 | | | | | |
| | 16 | | | | | | | 6 | | | | | |
| | 1960 11 | | | | | | | 11 | | | | | |
| | 16 | | | | | | | 16 | | | | | |
| | 1961 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |
| | 1962 11 | | | | | | | 1962 1 | | | | | |
| | 16 | | | | | | | 6 | | | | | |
| | | | | | | | | 11 | | | | | |
| | | | | | | | | 16 | | | | | |
| | | | | | | | | 21 | | | | | |
| | | | | | | | | 26 | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| X: Exceeds Allowable | | | | | | | | | | | | | |

TABLE 1-11. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 0 AND $V_g = 40$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δp | | Date | Bending Moment At Station | | | | Eng. Def. δp | |
|-----------------------------------|---|---|---|---|---|---|----------------------|---|---|--------|-----|---|---|--|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | | |
| JAN NOV APR L.A.=10% | 1955 10 15 1956 12 15 1957 12 19 1958 12 15 1959 12 15 | X X X X X X X X X | X X X X X X X X X | X X X X X X X X X | X X X X X X X X X | X X X X X X X X X | AUG L.A.= 86% | 1958 1 6 11 16 21 26 1959 1 6 11 16 21 26 1960 1 6 11 16 21 26 1961 1 6 11 16 21 26 1962 1 6 11 16 21 26 | | | | | | |
| FEB MAR DEC L.A.=0% | 1955 11 17 1956 14 17 1957 14 17 1958 11 17 1959 14 17 | X X X X X X X X X | X X X X X X X X X | X X X X X X X X X | X X X X X X X X X | X X X X X X X X X | | | | X X | | X X | X X | |
| MAY OCT L.A.= 30% | 1958 11 16 1959 11 16 1960 11 16 1961 11 16 1962 11 16 | | X X X X X X X X X | | X X X X X X X X X | X X X X X X X X X | | | | | | X | | |
| JULY L.A.= 100% | 1958 11 16 1959 11 16 1960 11 16 1961 11 16 1962 11 16 | | | | | | | SEPT JUNE L.A.= 60% | 1958 11 16 1959 11 21 1960 11 16 1961 11 16 1962 11 16 | | | X X X X X X X X X | X X X X X X X X X | |
| X: Exceeds Allowable | | | | | | | | | | | | | | |

| | Date | Bending Moment At Station | | | | Eng. Def. δ_p | | Date | Bending Moment At Station | | | | Eng. Def. δ_p |
|-----------|---------|------------------------------|-----|-----|-----|----------------------------|-----------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| JAN | 1955 10 | X | X | X | X | X | SEPT | 1958 11 | | | | | |
| NOV | 15 | X | X | X | X | X | JUNE | 16 | | | | | |
| APR | 1956 12 | X | X | X | X | X | L.A.= 50% | 1959 11 | | | | X | |
| | 15 | | X | | X | | | 16 | | X | X | X | |
| L.A.= 10% | 1957 12 | X | X | X | X | X | | 1960 11 | | X | | X | |
| | 19 | | X | X | X | X | | 16 | | | | | |
| | 1958 12 | X | X | X | X | X | | 1961 11 | X | X | X | X | |
| | 15 | X | X | X | X | X | | 16 | | | | | |
| | 1959 12 | | | | | | | 1962 11 | | | | | |
| | 15 | X | X | X | X | X | | 16 | | | | X | |
| FEB | 1955 11 | X | X | X | X | X | JULY | 1958 1 | | | | | |
| MAR | 17 | X | X | X | X | | | 6 | | | | | |
| DEC | 1956 11 | X | X | X | X | | L.A.= 83% | 11 | | | | | |
| | 17 | | X | X | X | X | | 16 | | | | | |
| L.A.= 0% | 1957 11 | X | X | X | X | X | | 21 | | X | | X | X |
| | 17 | X | X | X | X | X | | 26 | | | | | |
| | 1958 11 | X | X | X | X | X | | 1959 1 | | | | | |
| | 17 | X | X | X | X | X | | 6 | | | | | |
| | 1959 11 | X | X | X | X | | | 11 | | | | | |
| | 17 | X | X | X | X | X | | 16 | | | | X | |
| MAY | 1958 11 | | | | | | | 21 | | | | X | |
| OCT | 16 | | | | | | | 26 | X | X | | X | |
| | 1959 11 | | | | | | | 1960 1 | | X | | X | |
| L.A.= 30% | 16 | | X | | X | X | | 6 | | | | | |
| | 1960 11 | X | X | X | X | X | | 11 | | | | | |
| | 16 | | X | | X | | | 16 | | | | | |
| | 1961 11 | X | X | | X | | | 21 | | | | | |
| | 16 | | X | X | X | | | 26 | | | | | |
| | 1962 11 | X | X | X | X | X | | 1961 1 | | | | | |
| | 16 | | X | X | X | X | | 6 | | | | | |
| AUG | 1958 11 | | | | | | | 11 | | | | | |
| | 16 | | | | | | | 16 | | | | | |
| L.A.= 90% | 1959 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |
| | 1960 11 | | | | | | | 1962 1 | | | | | |
| | 16 | | | | | | | 6 | | | | | |
| | 1961 11 | | | | | | | 11 | | | | | |
| | 16 | | | | | | | 16 | | | | | |
| | 1962 11 | | X | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |

X: Exceeds Allowable

LAUNCH AVAILABILITY VERSUS MONTHS

— — — PP 130 MAR
 — — — PP 100 JAN
 — — — PP 70 MAY
 — · · — PP 30 SEP
 — x x — PP 0 AUG
 — x — PP (-20) JUL

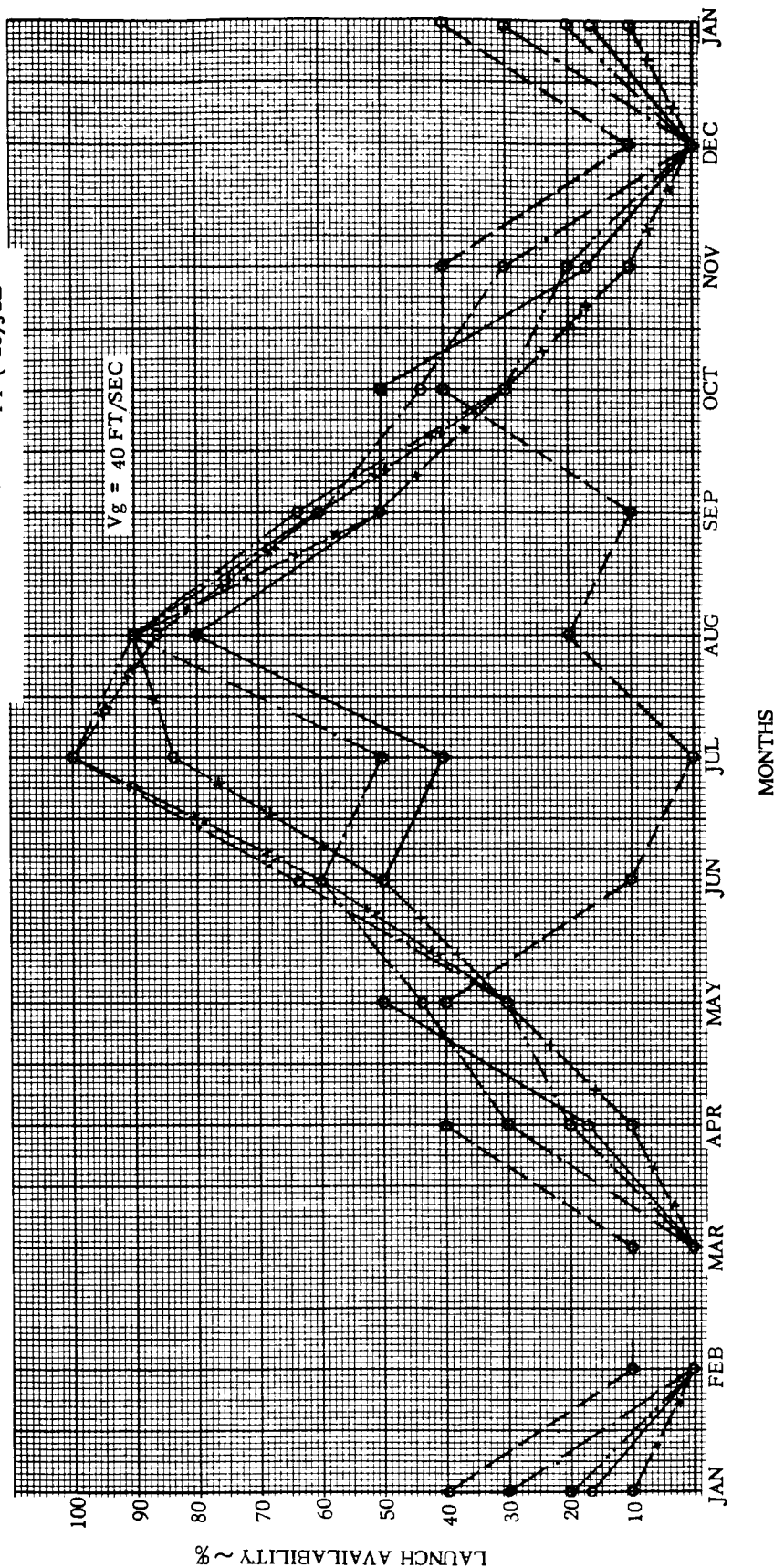


Figure 1-2. Comparison of Six Pitch Programs for Each Month of the Year

2W02ST

SECTION II

IMPROVED PERFORMANCE ON LAUNCH AVAILABILITY

2.1 GENERAL

This section presents, with graphs, tables, and equations, methods which will improve the launch capability of the Atlas/Centaur vehicle.

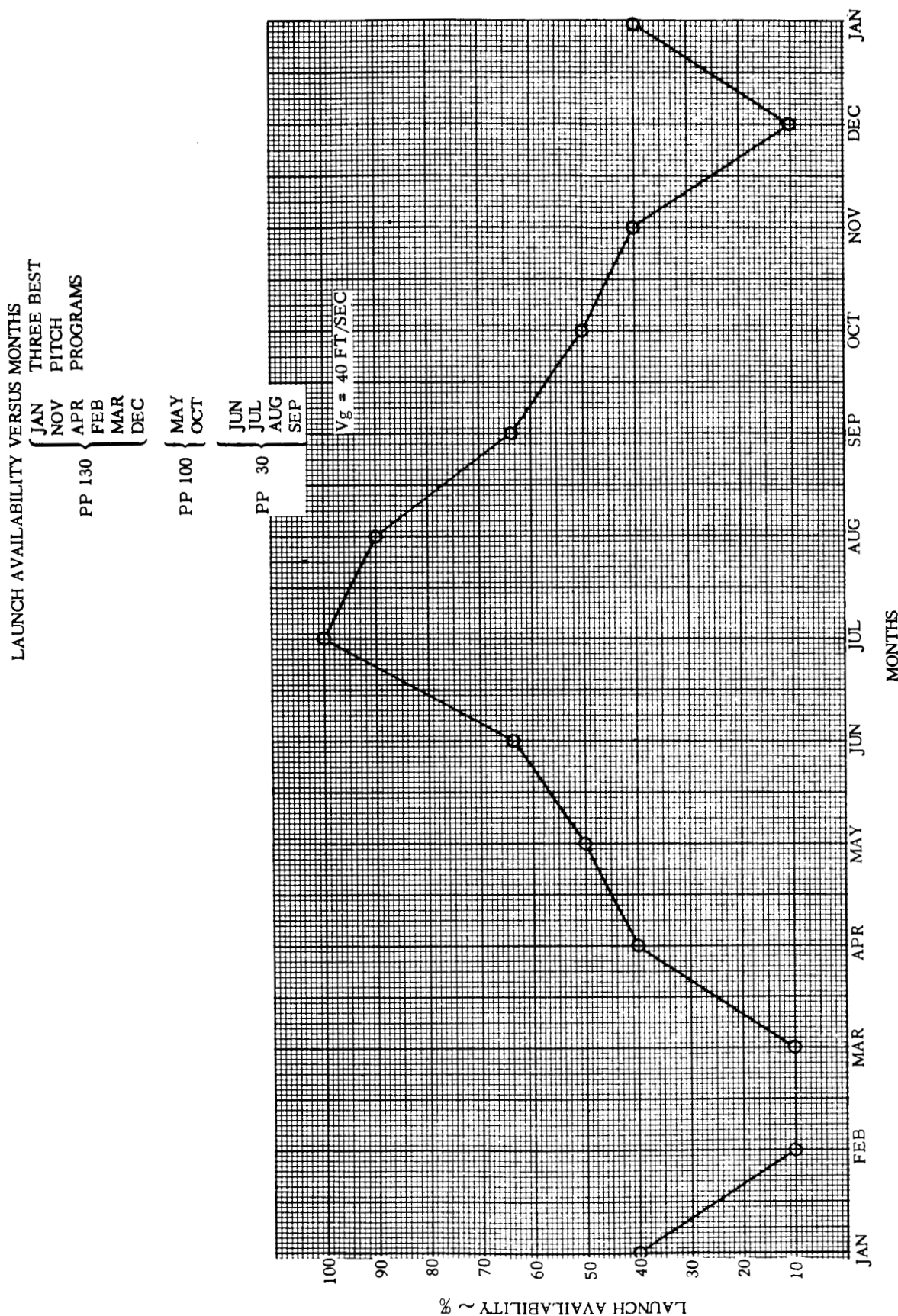
2.1.1 BEST PITCH PROGRAMS. By taking note of Figure 1-2, it can be observed that the best pitch programs are as follows:

- a. November
December
January PP 130
February
March
April
- b. May PP 100
October
- c. June
July PP 30
August
September

Using the three best pitch programs, Figure 2-1 was then obtained. This plot indicates the present best percent launch availability for the complete year.

2.1.2 INCREASE IN TANK PRESSURE. The following derivation will show how an increase in tank pressure will allow an increase in bending moment. The axial tensile stress in a tank is given as $\sigma_a = \frac{Pr}{2t}$ and the bending stress is given as $\sigma_b = \frac{M}{\pi r^2 t}$. Now let $\sigma_a = \sigma_b$ then $p = \frac{2M}{r^3 \pi}$.

If $p = 1$ psi and $r = 60$ " then $M = .340 \times 10^6$ in.-lb. This means that an increase in pressure of 1 psi will allow an increase in ultimate bending moment equal to $.340 \times 10^6$ in.-lb. Application of the factor of safety of 1.25 will produce a limit bending moment of $.272 \times 10^6$ in.-lb. per 1 psi increase in tank pressure. It may be noted from one of the SC 4020 Bending Moment plots that if $\Delta p = 1$ psi in the Atlas tank then only $\Delta p = 1/2$ psi is needed in the Centaur tank. Pitch Program 30 for the months of September and June will be used as an example and the results of increasing tank pressure is illustrated in Figure 2-2.



2W17ST

Figure 2-1. Envelope of the Best Pitch Programs During Each Month

The solid line in Figure 2-2 represents the present percent launch availability. The broken lines indicate increase in percent launch availability due to an increase in pressure in the Atlas and Centaur tanks.

2.1.3 REDUCTION IN THE GUST VELOCITY CRITERION. The gust velocity criterion for this study is 40 ft/sec. It was decided to reduce the gust velocity criterion to 30 ft/sec. and see how much the percent launch availability would be increased. The three best pitch programs were checked resulting in Tables 2-1 through 2-3. For additional information on reduction in gust velocity criterion see Note¹ on page 1-1.

Figure 2-3 plots the new launch availability curves for PP 130, PP 100, and PP 30. It may now be observed that only PP 130 and PP 30 are needed if $V_g = 30$ ft/sec. is used. Figure 2-4 shows the comparison between $V_g = 40$ ft/sec. and $V_g = 30$ ft/sec.

28 December 1964

$\Delta p = 0$ $\Delta p = 0$
 $\Delta p = .625$ PSI $\Delta p = 1.250$ PSI
 $\Delta p = 1.250$ PSI $\Delta p = 2.500$ PSI
 $\Delta p = 1.875$ PSI $\Delta p = 3.750$ PSI
 $\Delta p = 2.500$ PSI $\Delta p = 5.000$ PSI

CENTAUR ATLAS

Δp : INCREASE
 IN PRESSURE

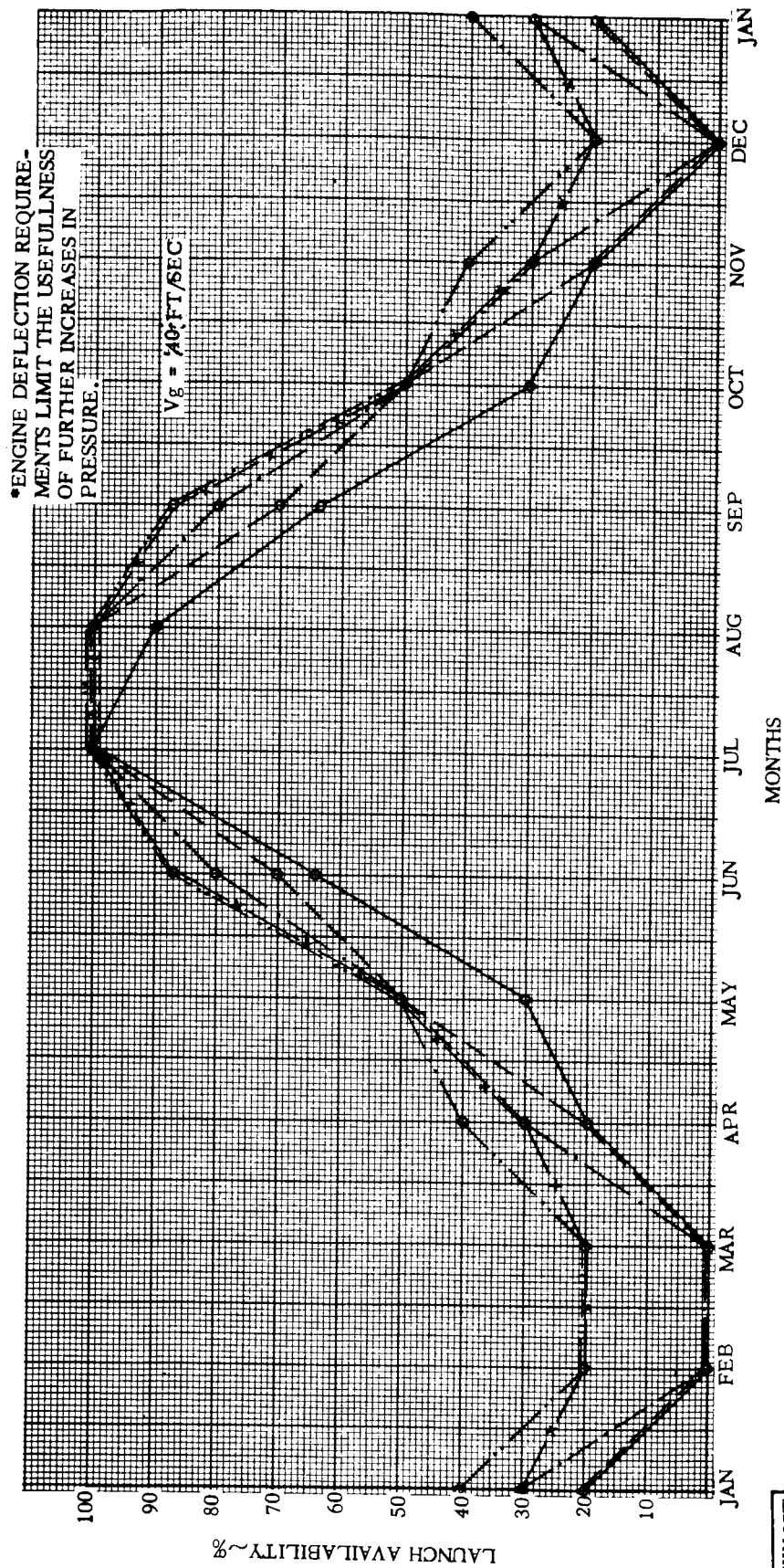


Figure 2-2. Effects of Tank Pressure on Launch Availability Versus Months for PP 30

28 December 1964

TABLE 2-1. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 130 AND $V_g = 30$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δ_p | | Date | Bending Moment At Station | | | | Eng. Def. δ_p |
|------------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|-----------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| JAN NOV APR L.A.= 50% | 1955 10 | | | | | | SEPT JUNE L.A.=60% | 1958 11 | | | | | |
| | 15 | | X | | | | | 16 | | | | | |
| | 1956 12 | | X | | X | | | 1959 6 | | | | | |
| | 15 | | | | | | | 11 | | | | | |
| | 1957 12 | | | | | | | 1960 11 | | X | | X | |
| | 19 | | | | | | | 16 | | | | | |
| | 1958 12 | X | X | X | X | | | 1961 11 | | X | | X | |
| | 15 | X | X | X | X | | | 16 | | | | | |
| MAY OCT L.A.= 80% | 1959 12 | | | | | | FEB MAR DEC L.A.=33% | 1962 11 | | X | | X | X |
| | 15 | X | X | X | X | X | | 16 | X | | | X | X |
| | 1958 11 | | | | | | | 1955 2 | | | | | |
| | 16 | | | | | | | 5 | | X | X | X | X |
| | 1959 11 | | | | | | | 11 | X | X | X | X | |
| | 16 | | | | | | | 17 | X | X | X | X | |
| | 1960 11 | X | X | | | | | 23 | | | | | |
| | 16 | | | | | | | 26 | | | | | |
| JULY L.A.= 50% | 1961 11 | X | X | X | X | | 1956 2 | 5 | X | X | X | X | |
| | 16 | | | | | | | 11 | X | X | X | X | X |
| | 1962 11 | | | | | | | 14 | | | | | |
| | 16 | | | | | | | 17 | | | | | |
| | 1958 11 | | | | | | | 23 | | | | | |
| | 16 | | X | | X | X | | 1957 2 | | | | | |
| | 1959 11 | | | | | | | 5 | | | | | |
| | 16 | | X | | X | | | 11 | | | | | |
| AUG L.A.= 80% | 1960 11 | | X | | X | | 1958 1 | 17 | | X | | X | |
| | 16 | | | | | | | 20 | | X | | X | |
| | 1961 11 | | X | | | | | 26 | X | X | X | X | |
| | 16 | | X | | X | | | 1959 2 | | X | | X | |
| | 1962 11 | | X | | X | | | 5 | X | X | | X | |
| | 16 | | X | | X | | | 11 | | X | | X | |
| | 1958 11 | | X | | | | | 17 | | X | | X | |
| | 16 | | | | | | | 20 | X | X | X | X | X |
| | 1959 11 | | | | | | 1959 2 | 25 | X | X | X | X | |
| | 16 | | | | | | | | | | | | |
| | 1960 11 | | X | | X | X | | | | | | | |
| | 16 | | | | | | | | | | | | |
| | 1961 11 | | | | | | | | | | | | |
| | 16 | | | | | | | | | | | | |
| | 1962 11 | | | | | | | | | | | | |
| | 16 | | | | | | | | | | | | |

X: Exceeds Allowable

| | Date | Bending Moment At Station | | | | Eng. Def. δ_p | | Date | Bending Moment At Station | | | | Eng. Def. δ_p |
|-----------|---------|------------------------------|-----|-----|-----|----------------------------|-------------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| FEB | 1955 11 | X | X | X | X | | SEPT | 1958 11 | | | | | |
| MAR | 17 | X | X | X | X | | JUNE | 16 | | | | | |
| DEC | 1956 11 | X | X | X | X | X | L.A.=60% | 1959 11 | | | | | |
| L.A.= 10% | 17 | | | | | | | 21 | | | | | |
| | 1957 11 | | X | | | | | 1960 11 | | X | | X | |
| | 17 | | X | | X | | | 16 | | | | | |
| | 1958 11 | X | X | | | | | 1961 11 | | X | | X | |
| | 17 | X | X | X | X | X | | 16 | | | | | |
| | 1959 11 | | X | | | | | 1962 11 | | X | | X | X |
| | 17 | | X | X | X | | | 16 | | X | | X | |
| MAY | 1958 11 | | | | | | JAN | 1955 3 | | | | | |
| OCT | 16 | | | | | | NOV | 6 | | X | | | |
| L.A.=70% | 1959 11 | | | | | | APR | 10 | | X | | | |
| | 16 | | | | | | L.A.= 46.7% | 15 | | | | | |
| | 1960 11 | | X | | X | | | 21 | X | X | X | X | |
| | 16 | | | | | | | 27 | X | X | X | X | X |
| | 1961 11 | | X | | | | | 1956 3 | | | | | |
| | 16 | | | | | | | 6 | | | | | |
| | 1962 11 | | X | | | | | 12 | | X | | X | |
| | 16 | | | | | | | 15 | | | | | |
| JULY | 1958 11 | | | | | | | 21 | | X | | X | |
| L.A.=90% | 16 | | | | | | | 27 | | | | X | |
| | 1959 11 | | | | | | | 1957 3 | | | | | |
| | 16 | | | | | | | 6 | X | X | X | X | X |
| | 1960 11 | | | | | | | 12 | | | | | |
| | 16 | | | | | | | 19 | | | | | |
| | 1961 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 27 | | | | | |
| | 1962 11 | | | | | | | 1958 3 | X | X | X | X | X |
| | 16 | | X | | | | | 6 | X | X | X | X | X |
| AUG | 1958 11 | | | | | | | 12 | X | X | X | X | |
| L.A.= 90% | 16 | | | | | | | 15 | X | X | X | X | |
| | 1959 11 | | | | | | | 21 | X | X | X | X | X |
| | 16 | | | | | | | 27 | X | X | X | X | X |
| | 1960 11 | | X | | | | | 1959 3 | | | | | |
| | 16 | | | | | | | 6 | | X | | X | |
| | 1961 11 | | | | | | | 12 | | | | | |
| | 16 | | | | | | | 15 | X | X | X | X | X |
| | 1962 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 27 | | | | | |

TABLE 2-3. "X" CHART OF AC-7 TO AC-15 % LAUNCH AVAILABILITY
USING PITCH PROGRAM 30 AND $V_g = 30$ FT/SEC

| | Date | Bending Moment At Station | | | | Eng. Def. δ_p | | Date | Bending Moment At Station | | | | Eng. Def. δ_p |
|-----------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|------------------------------|---------|------------------------------|-----|-----|-----|----------------------------|
| | | 219 | 410 | 568 | 770 | | | | 219 | 410 | 568 | 770 | |
| JAN NOV APR L.A.=30% | 1955 10 | | X | | X | | AUG L.A.=100% | 1958 11 | | | | | |
| | 15 | | X | | X | | | 16 | | | | | |
| | 1956 12 | X | X | X | X | X | | 1959 11 | | | | | |
| | 15 | | | | | | | 16 | | | | | |
| | 1957 12 | | | | | | | 1960 11 | | | | | |
| | 19 | | X | | X | | | 16 | | | | | |
| | 1958 12 | X | X | X | X | X | | 1961 11 | | | | | |
| FEB MAR DEC L.A.=10% | 15 | X | X | X | X | X | SEPT JUNE L.A.=90% | 16 | | | | | |
| | 1959 12 | | | | | | | 1962 11 | | | | | |
| | 15 | X | X | X | X | X | | 16 | | | | | |
| | 1955 11 | X | X | X | X | | | 1958 1 | | | | | |
| | 17 | X | X | X | X | | | 6 | | | | | |
| | 1956 14 | | X | | X | | | 11 | | | | | |
| | 17 | | | | | | | 16 | | | | | |
| | 1957 14 | | X | X | X | | | 21 | | | | | |
| | 17 | | X | | X | | | 26 | | | | | |
| | 1958 11 | X | X | | X | | | 1959 1 | | | | | |
| | 17 | X | X | X | X | X | | 6 | | | | | |
| | 1959 14 | | X | | | | | 11 | | | | | |
| | 17 | X | X | X | X | | | 16 | | | | | |
| MAY OCT L.A.=50% | 1958 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |
| | 1959 11 | | | | | | | 1960 1 | | | | | |
| | 16 | | X | | X | | | 6 | | | | | |
| | 1960 11 | X | X | X | X | | | 11 | | | | | |
| | 16 | | | | | | | 16 | | | | | |
| | 1961 11 | | X | | | | | 21 | | X | X | X | |
| JULY L.A.=100% | 16 | | | | | | | 26 | | | | | |
| | 1962 11 | | X | | X | | | 1961 1 | | | | | |
| | 16 | | X | | X | | | 6 | | X | | X | |
| | 1958 11 | | | | | | | 11 | X | X | X | X | |
| | 16 | | | | | | | 16 | | | | | |
| | 1959 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |
| | 1960 11 | | | | | | | 1962 1 | | | | | |
| | 16 | | | | | | | 6 | | | | | |
| | 1961 11 | | | | | | | 11 | | | | | |
| | 16 | | | | | | | 16 | | | | | |
| | 1962 11 | | | | | | | 21 | | | | | |
| | 16 | | | | | | | 26 | | | | | |

X: Exceeds Allowable

$V_g - 30 \text{ FT/SEC}$

--- PP 130
--- PP 100
--- PP 30

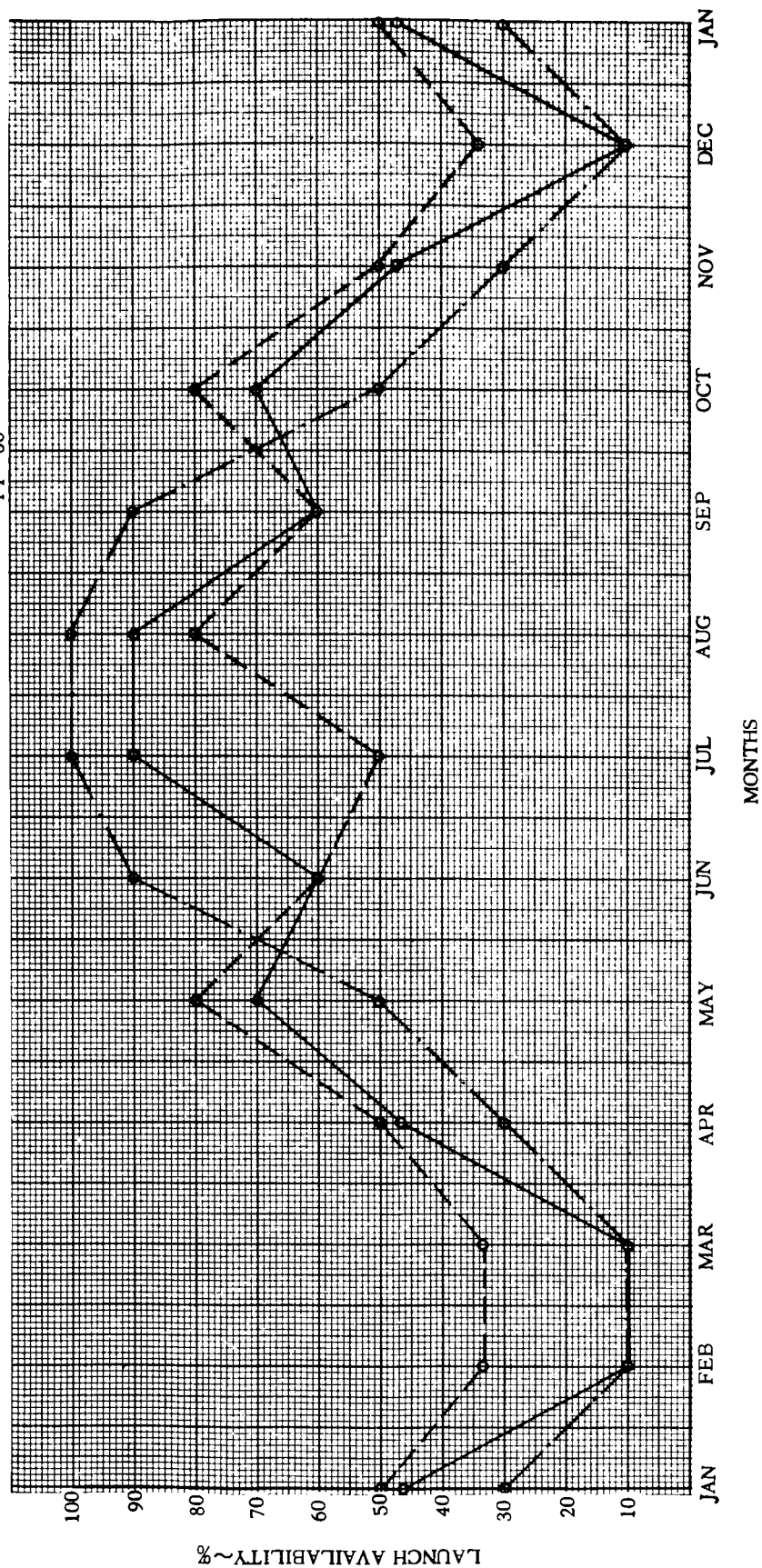
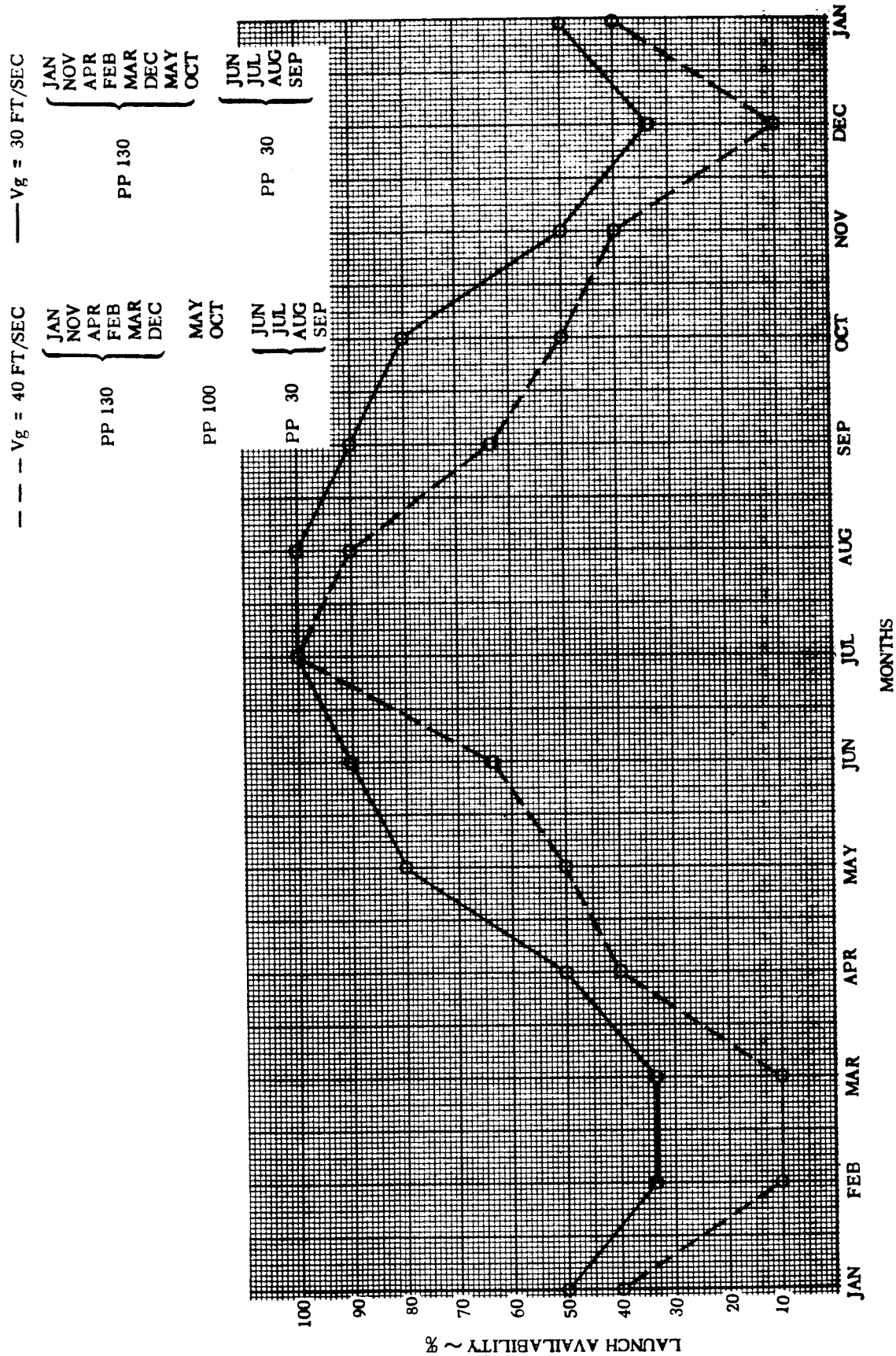


Figure 2-3. Launch Availability Versus Months Using a 30 ft/sec Gust Criterion

2W19ST



2W206T

Figure 2-4. Comparison of Launch Availability for 30 ft/sec and 40 ft/sec Gust Criterion

SECTION III

PRESENT PITCH PROGRAMS

3.1 INFORMATION FROM EXISTING PITCH PROGRAMS

3.1.1 TIME IN FLIGHT FOR MAXIMUM BENDING MOMENTS. It was desired to find the time after liftoff when the maximum aerodynamic loading occurred. Referring to Figures A-1 and A-2 in the Appendix it may be noted that the maximum bending moment occurs at 64 seconds for Stations 410 and 770. By checking Atlas/Centaur (AC-7) Pitch Program Investigation Plots for 100 wind profiles Figures 3-1 and 3-2 were obtained. From Figure 3-1 for Station 410 the average time inflight for maximum bending moment was 69.55 seconds and 74 percent of the maximum bending moments occurred between 65 and 75 seconds. From Figure 3-2 for Station 770 the average time inflight for maximum bending moment was 71.48 seconds and 63 percent of the maximum bending moments occurred in between 65 and 75 seconds. From the preceding information it was decided to analyze the following increment of time $\Delta t = 65$ to 75 seconds.

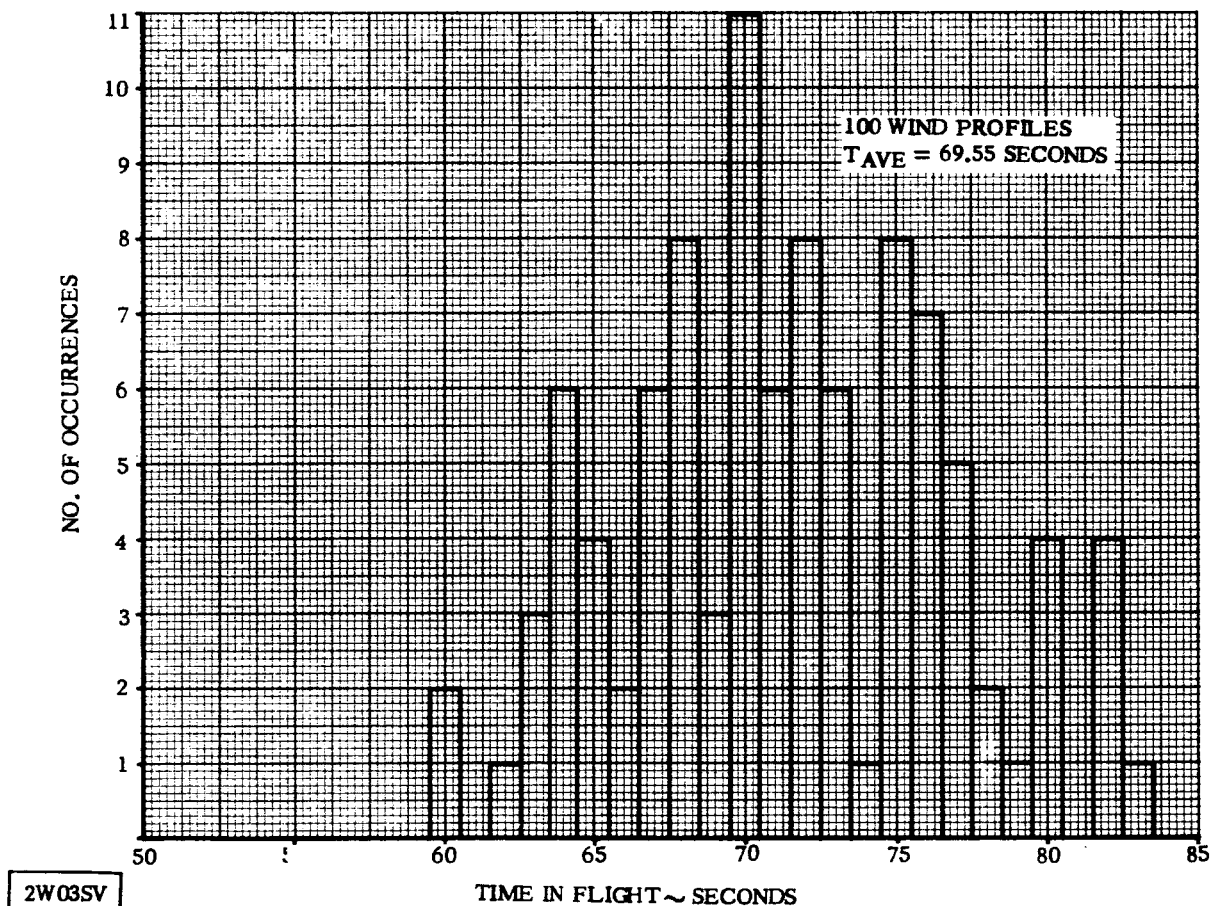
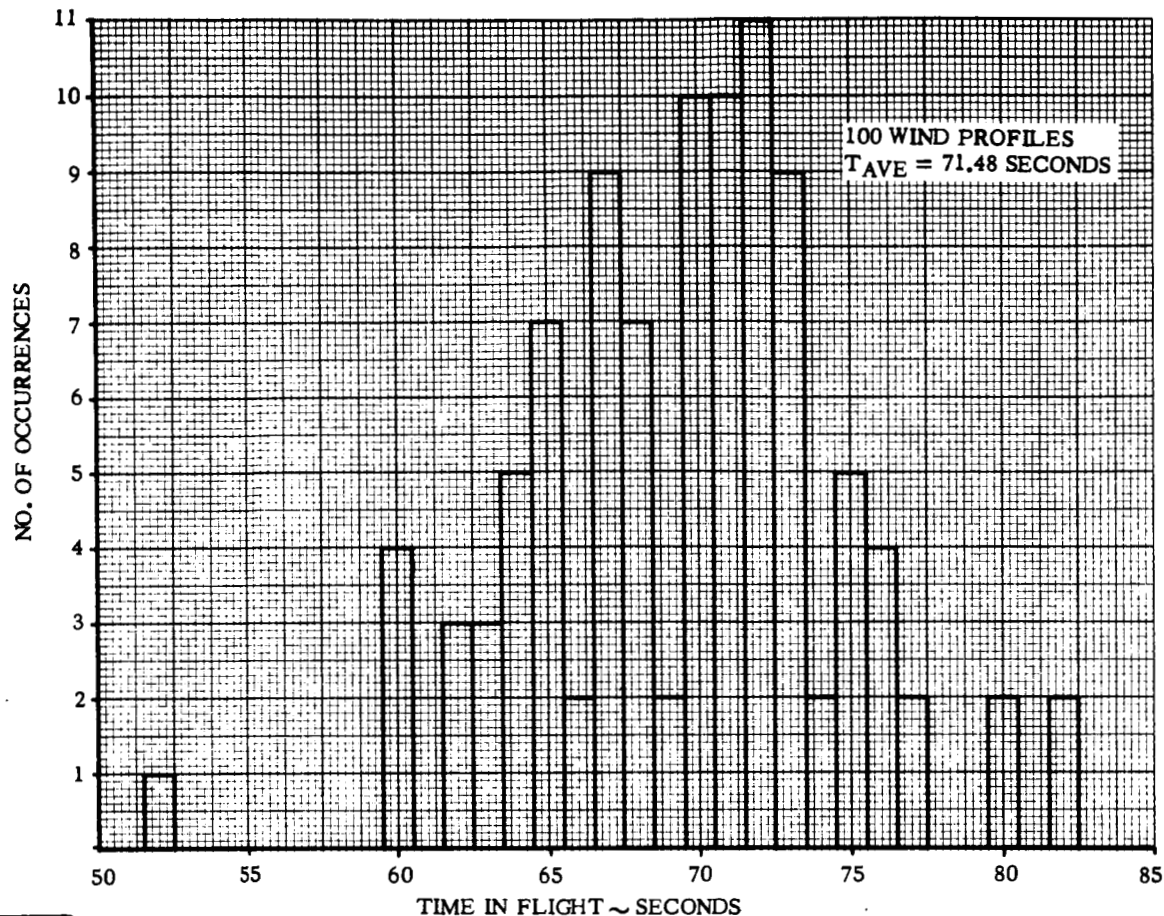


Figure 3-1. Histogram of Time In Flight for Maximum Bending Moment at Station 410



2W04SV

Figure 3-2. Histogram of Time In Flight for Maximum Bending Moment at Station 770

3.1.2 BAND WIDTH FOR αq and βq . Pitch Program 30 which was designed for September and June will be used in this section for sample calculations and plots. Referring to Figures A-3, A-4 in the Appendix, the plots of αq and βq versus time in flight are shown for one particular September wind. The band widths are shown for 65 to 75 seconds inflight. The band width is defined as twice the maximum value (or referred to as plus and minus the maximum value) of the variable (αq or βq) between 65 and 75 seconds. Figures 3-3 and 3-4 are Histograms for αq and βq band widths, and were obtained by using 30 wind profiles. The plots of % Launch Availability versus Band Width shown in Figures 3-5 and 3-6 were obtained from Figures 3-3 and 3-4 by the following method: If the % Launch Availability is desired for a particular band width value then $\% \text{ L.A.} = \frac{\sum N_i \times 100}{N_{\text{TOTAL}}}$ where $\sum N_i$ is the sum of occurrences up to and including the desired band width and N_{TOTAL} is sum of all the occurrences.

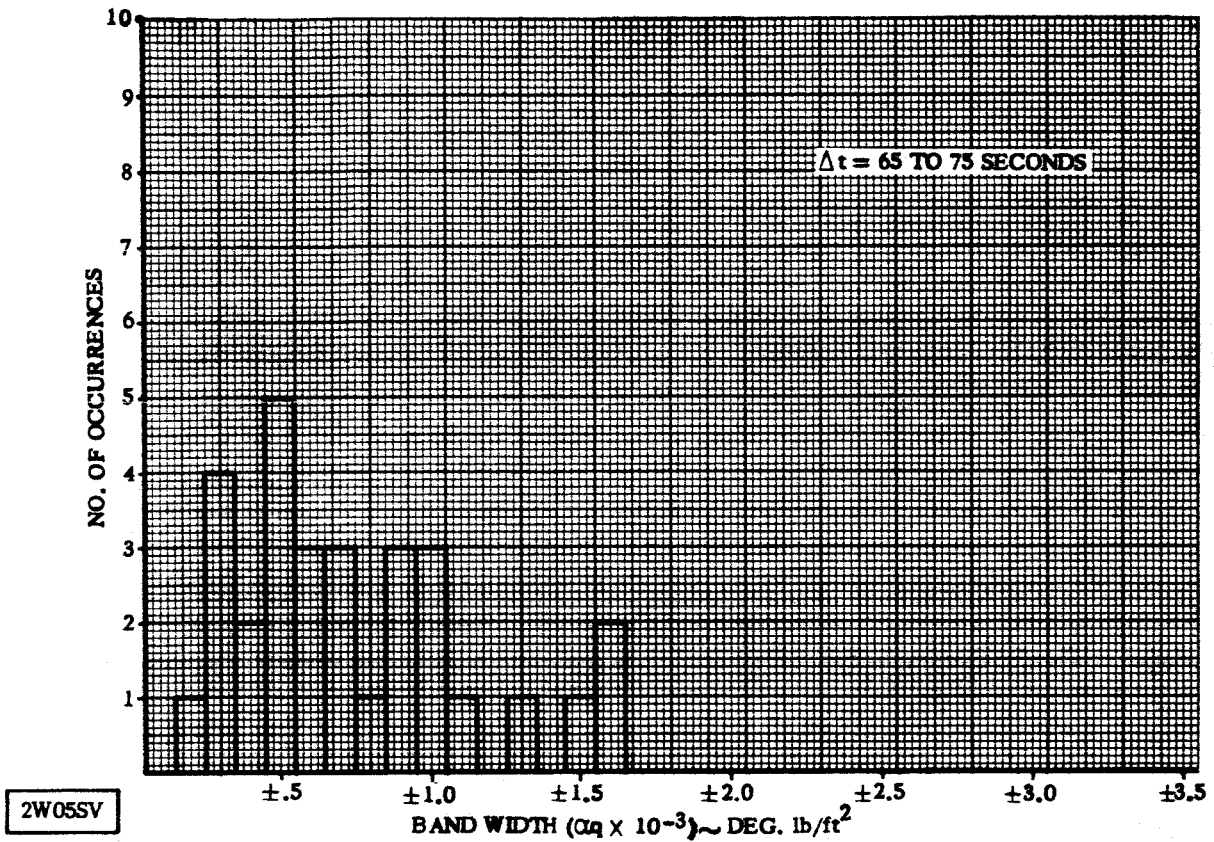


Figure 3-3. Histogram of α_q for PP30 September and June

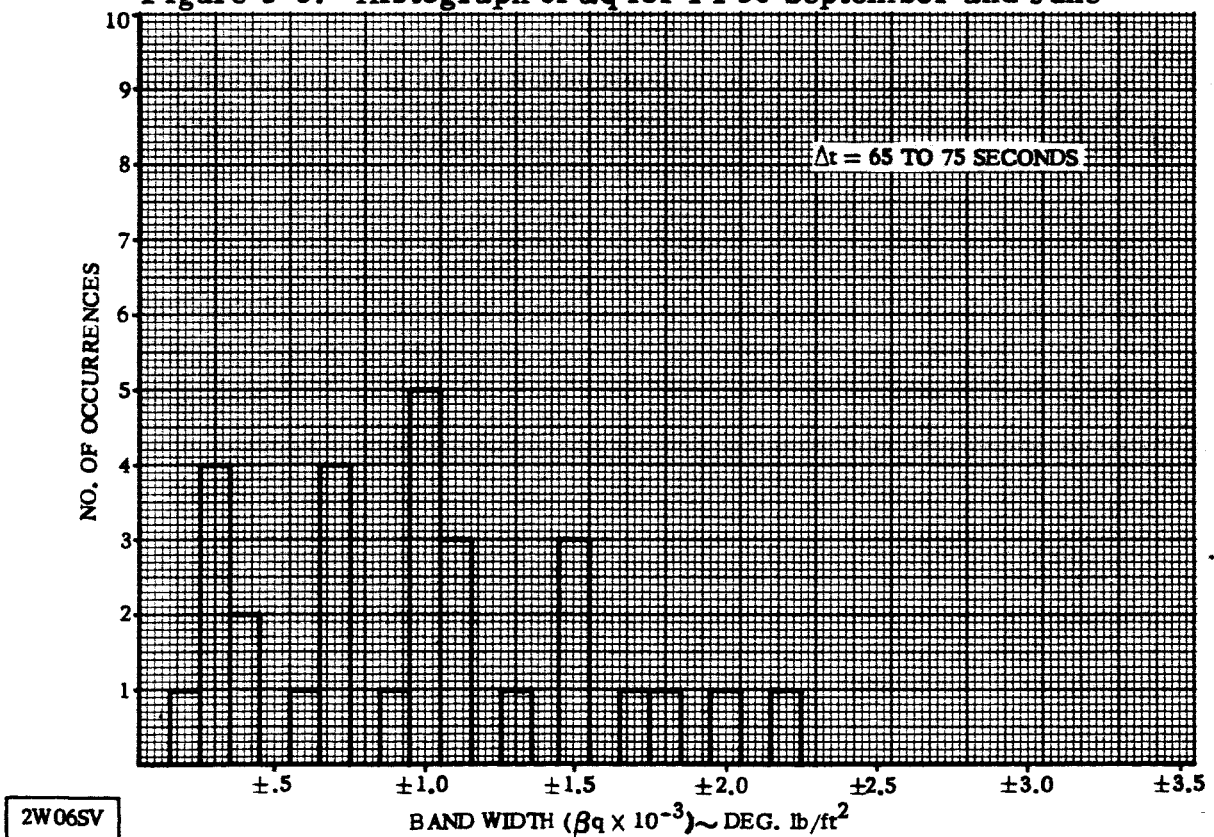
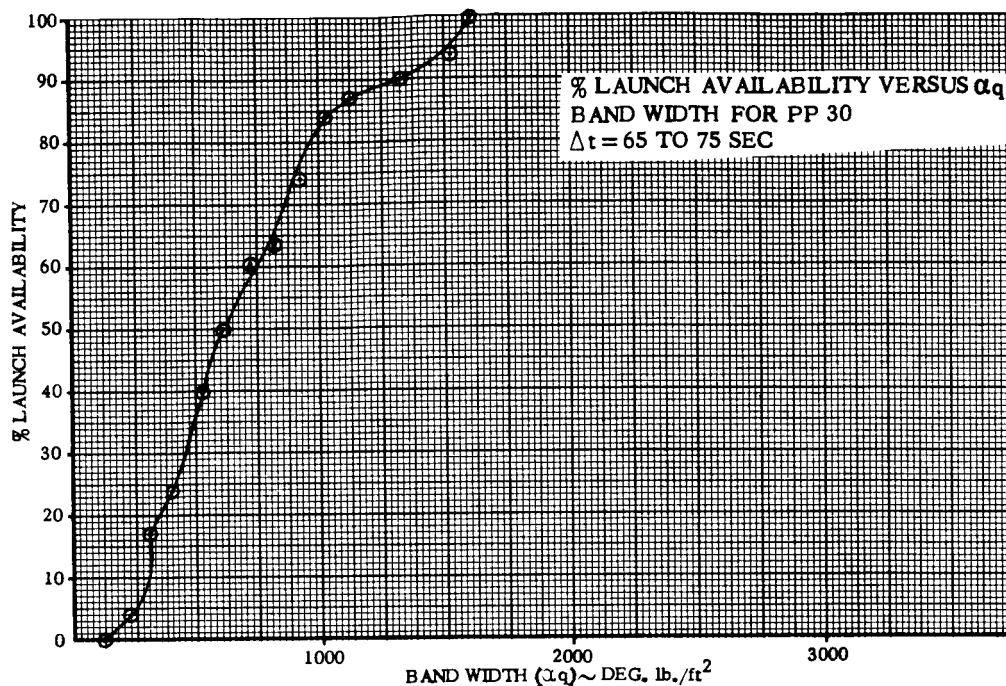
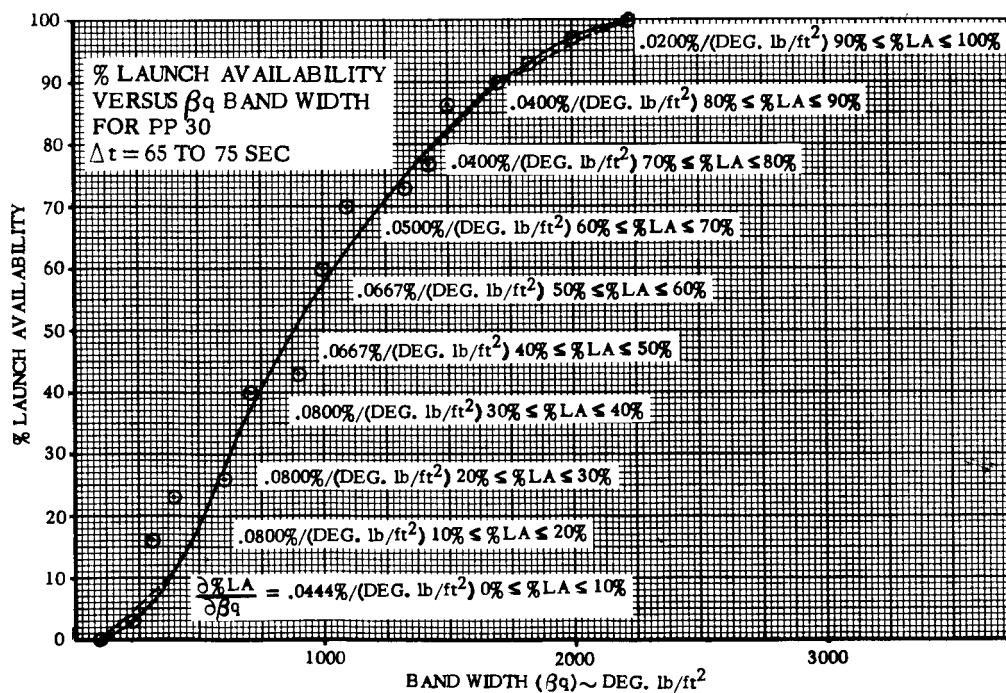


Figure 3-4. Histogram of β_q for PP30 September and June



2W07SV

Figure 3-5. % Launch Availability Versus αq Band Width for PP30



2W08SV

Figure 3-6. % Launch Availability Versus βq Band Width for PP30

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Now observing Figures 3-5 and 3-6 it may be noted that the βq band width is critical since the % Launch Availability is lower for a particular βq band width than it is for the same αq band width. The % Launch Availability versus βq band width curve was then approximated by several straight lines and the slopes of these lines were then calculated as shown in Figures 3-6. These slopes are actually the quantity $\frac{\partial \% LA}{\partial \beta q}$ and they are summarized in Tables 3-1 to 3-6.

3.1.3 BENDING MOMENTS NEEDED FOR SPECIFIC % LAUNCH AVAILABILITY. From Reference 4 at 68 seconds inflight the bending moment at Station 410 is 1.0383×10^6 in.-lbs., the bending moment at Station 770 is 1.3529×10^6 in.-lbs., and $\beta q = 762.44$ deg. lbs/ft². AC-5 was used since its configuration is very similar to AC-7 thru AC-15. Using the preceding values then the:

$$\frac{\partial BM_{410}}{\partial \beta q} = \frac{1.0383 \times 10^6 \text{ in.-lbs.}}{762.44 \text{ deg. lb/ft}^2} = 1.3618 \times 10^3 \frac{\text{in.-lbs.}}{\text{deg. lb/ft}^2} \text{ and the}$$

$$\frac{\partial BM_{770}}{\partial \beta q} = \frac{1.3529 \times 10^6 \text{ in.-lbs.}}{762.44 \text{ deg. lb/ft}^2} = 1.7744 \times 10^3 \frac{\text{in.-lbs.}}{\text{deg. lb/ft}^2}$$

Next the quantities $\frac{\partial BM}{\partial \% LA} = \left(\frac{\partial BM}{\partial \beta q} \right) \left(\frac{\partial \% LA}{\partial \beta q} \right)$ were calculated for Station 410 and 770

and they are summarized in Tables 3-1 to 3-6.

TABLE 3-1. PARTIAL DERIVATIVE OF % L.A. WITH RESPECT TO βq AND PARTIAL DERIVATIVE OF BENDING MOMENT WITH RESPECT TO % L.A. FOR (PP130) (FEB, MAR & DEC) (65 SEC < t < 75 SEC)

| % Launch Availability (%) | $\frac{\partial \% LA}{\partial \beta q}$ (%/deg. lb/ft ²) | $\frac{\partial BM_{410} \times 10^{-6}}{\partial \% LA}$ (in.-lbs/% LA) | $\frac{\partial BM_{770} \times 10^{-6}}{\partial \% LA}$ (in.-lbs/% LA) |
|---------------------------|---|---|---|
| 0-10 | .0333 | .0409 | .0533 |
| 10-20 | .0333 | .0409 | .0533 |
| 20-30 | .0400 | .0340 | .0443 |
| 30-40 | .2000 | .0068 | .0089 |
| 40-50 | .0500 | .0272 | .0357 |
| 50-60 | .0500 | .0272 | .0357 |
| 60-70 | .0250 | .0545 | .0710 |
| 70-80 | .1333 | .0102 | .0133 |
| 80-90 | .0444 | .0307 | .0400 |
| 90-100 | .0067 | .2033 | .2648 |

TABLE 3-2. PARTIAL DERIVATIVE OF % L.A. WITH RESPECT TO βq AND PARTIAL DERIVATIVE OF BENDING MOMENT WITH RESPECT TO % L.A. FOR (PP100) (JAN, NOV & APR) (65 SEC < t < 75 SEC)

| % Launch Availability (%) | $\frac{\partial \% \text{ LA}}{\partial \beta q}$ (%/deg. lb/ft ²) | $\frac{\partial \text{BM}_{410} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) | $\frac{\partial \text{BM}_{770} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) |
|---------------------------|---|--|--|
| 0-10 | .0200 | .0680 | .0890 |
| 10-20 | .0500 | .0272 | .0357 |
| 20-30 | .1000 | .0136 | .0177 |
| 30-40 | .0400 | .0340 | .0443 |
| 40-50 | .0667 | .0203 | .0265 |
| 50-60 | .1333 | .0102 | .0133 |
| 60-70 | .0769 | .0177 | .0231 |
| 70-80 | .0308 | .0442 | .0576 |
| 80-90 | .0211 | .0645 | .0840 |
| 90-100 | .0067 | .2033 | .2648 |

TABLE 3-3. PARTIAL DERIVATIVE OF % L.A. WITH RESPECT TO βq AND PARTIAL DERIVATIVE OF BENDING MOMENT WITH RESPECT TO % L.A. FOR (PP70) (MAY & OCT) (65 SEC < t < 75 SEC)

| % Launch Availability (%) | $\frac{\partial \% \text{ LA}}{\partial \beta q}$ (%/deg. lb/ft ²) | $\frac{\partial \text{BM}_{410} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) | $\frac{\partial \text{BM}_{770} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) |
|---------------------------|---|--|--|
| 0-10 | .0800 | .0170 | .0222 |
| 10-20 | .0800 | .0170 | .0222 |
| 20-30 | .1333 | .0102 | .0133 |
| 30-40 | .1000 | .0136 | .0177 |
| 40-50 | .0800 | .0170 | .0222 |
| 50-60 | .0800 | .0170 | .0222 |
| 60-70 | .0571 | .0238 | .0310 |
| 70-80 | .0571 | .0238 | .0310 |
| 80-90 | .0333 | .0409 | .0533 |
| 90-100 | .0082 | .1661 | .2164 |

TABLE 3-4. PARTIAL DERIVATIVE OF % L.A. WITH RESPECT TO βq AND PARTIAL DERIVATIVE OF BENDING MOMENT WITH RESPECT TO % L.A. FOR (PP30) (SEPT. & JUNE) (65 SEC < t < 75 SEC)

| % Launch Availability (%) | $\frac{\partial \% \text{ LA}}{\partial \beta q}$ (%/deg. lb/ft ²) | $\frac{\partial \text{BM}_{410} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) | $\frac{\partial \text{BM}_{770} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) |
|---------------------------|---|--|--|
| 0-10 | .0444 | .0307 | .0400 |
| 10-20 | .0800 | .0170 | .0222 |
| 20-30 | .0800 | .0170 | .0222 |
| 30-40 | .0800 | .0170 | .0222 |
| 40-50 | .0667 | .0204 | .0266 |
| 50-60 | .0667 | .0204 | .0266 |
| 60-70 | .0500 | .0272 | .0357 |
| 70-80 | .0400 | .0340 | .0443 |
| 80-90 | .0400 | .0340 | .0443 |
| 90-100 | .0200 | .0680 | .0890 |

TABLE 3-5. PARTIAL DERIVATIVE OF % L.A. WITH RESPECT TO βq AND PARTIAL DERIVATIVE OF BENDING MOMENT WITH RESPECT TO % L.A. FOR (PP0) (AUG) (65 SEC < t < 75 SEC)

| % Launch Availability (%) | $\frac{\partial \% \text{ LA}}{\partial \beta q}$ (%/deg. lb/ft ²) | $\frac{\partial \text{BM}_{410} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) | $\frac{\partial \text{BM}_{770} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) |
|---------------------------|---|--|--|
| 0-10 | .1333 | .0102 | .0133 |
| 10-20 | .1000 | .0136 | .0177 |
| 20-30 | .0667 | .0204 | .0266 |
| 30-40 | .1000 | .0136 | .0177 |
| 40-50 | .2000 | .0068 | .0089 |
| 50-60 | .1000 | .0136 | .0177 |
| 60-70 | .0800 | .0170 | .0222 |
| 70-80 | .1000 | .0136 | .0177 |
| 80-90 | .1333 | .0102 | .0133 |
| 90-100 | .0108 | .1261 | .1643 |

TABLE 3-6. PARTIAL DERIVATIVE OF % L.A. WITH RESPECT TO βq AND PARTIAL DERIVATIVE OF BENDING MOMENT WITH RESPECT TO % L.A. FOR (PP-20) (JULY) (65 SEC < t < 75 SEC)

| % Launch Availability (%) | $\frac{\partial \% \text{ LA}}{\partial \beta q}$ (%/deg. lb/ft ²) | $\frac{\partial \text{BM}_{410} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) | $\frac{\partial \text{BM}_{770} \times 10^{-6}}{\partial \% \text{ LA}}$ (in.-lbs/% LA) |
|---------------------------|---|--|--|
| 0-10 | .0500 | .0272 | .0357 |
| 10-20 | .0571 | .0238 | .0310 |
| 20-30 | .0800 | .0170 | .0222 |
| 30-40 | .1333 | .0102 | .0133 |
| 40-50 | .1333 | .0102 | .0133 |
| 50-60 | .0800 | .0170 | .0222 |
| 60-70 | .1333 | .0102 | .0133 |
| 70-80 | .2000 | .0068 | .0089 |
| 80-90 | .0444 | .0307 | .0400 |
| 90-100 | .0129 | .1056 | .1376 |

Now using PP30 for September and June the % L.A. = 63% for $V_g = 40$ ft/sec, from Table 1-10, and the present available bending moment at Station 770 = 5.30×10^6 in.-lbs. Using the above information and Table 3-4 the following calculation will show how much bending moment is needed for % L.A. = 100% at Station 770 in September and June:

$$\begin{aligned}
 \text{BM}_{\% \text{ LA} = 100\%} &= \text{BM}_{\% \text{ LA} = 63\%} + \frac{\partial \text{BM}}{\partial \% \text{ LA}} (70\% - 63\%) + \frac{\partial \text{BM}}{\partial \% \text{ LA}} (80\% - 70\%) \\
 &\quad 60\% \leq \% \text{ LA} \leq 70 \quad 70\% \leq \% \text{ LA} \leq 80 \\
 &\quad + \frac{\partial \text{BM}}{\partial \% \text{ LA}} (90\% - 80\%) + \frac{\partial \text{BM}}{\partial \% \text{ LA}} (100\% - 90\%) \\
 &\quad 80\% \leq \% \text{ LA} \leq 90\% \quad 90\% \leq \% \text{ LA} \leq 100\% \\
 \text{BM}_{\% \text{ LA} = 100\%} &= 5.3 \times 10^6 \text{ in.-lbs.} + (.0357 \times 10^6)(7) \text{ in.-lbs.} + (.0443 \times 10^6)(10) \text{ in.-lbs.} \\
 &\quad + (.0443 \times 10^6)(10) \text{ in.-lbs.} + (.0890 \times 10^6)(10) \text{ in.-lbs.} \\
 \text{BM}_{\% \text{ LA} = 100\%} &= 7.32 \times 10^6 \text{ in.-lbs.}
 \end{aligned}$$

Using similar calculations for all six pitch programs so that 30 samples would be available for each month, the bending moments needed for specific percent launch availabilities for Stations 410 and 770 using gust velocities of 40 ft/sec. and 30 ft/sec. are shown in Figures 3-7 to 3-10. It should be noted that launch availabilities quoted in this section are less than optimum since the pitch programs listed on page 1-2 were used.

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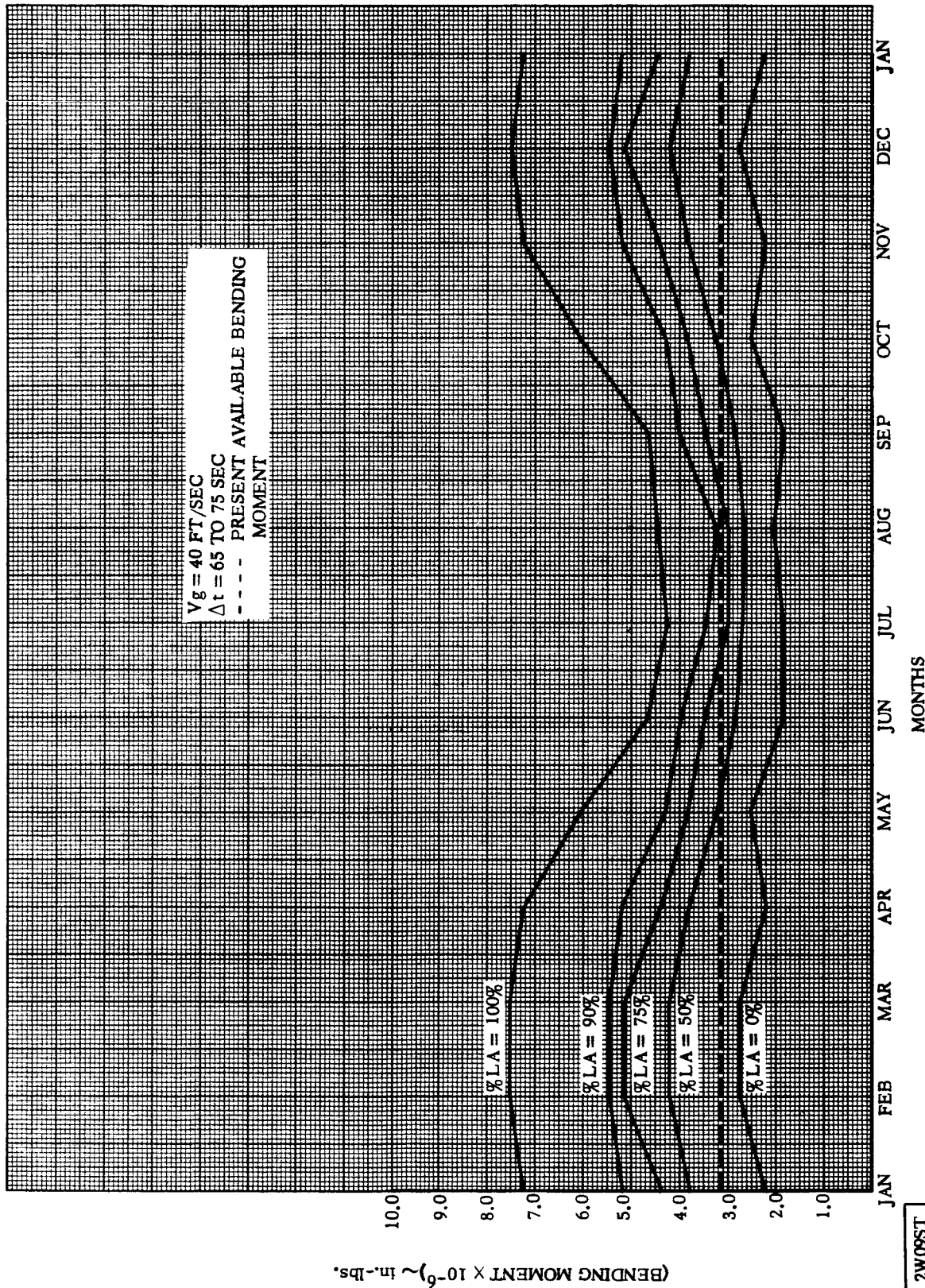


Figure 3-7. Bending Moments Needed for Specific Launch Availability Versus Months for Station 410 (40 ft/sec)

2W09ST

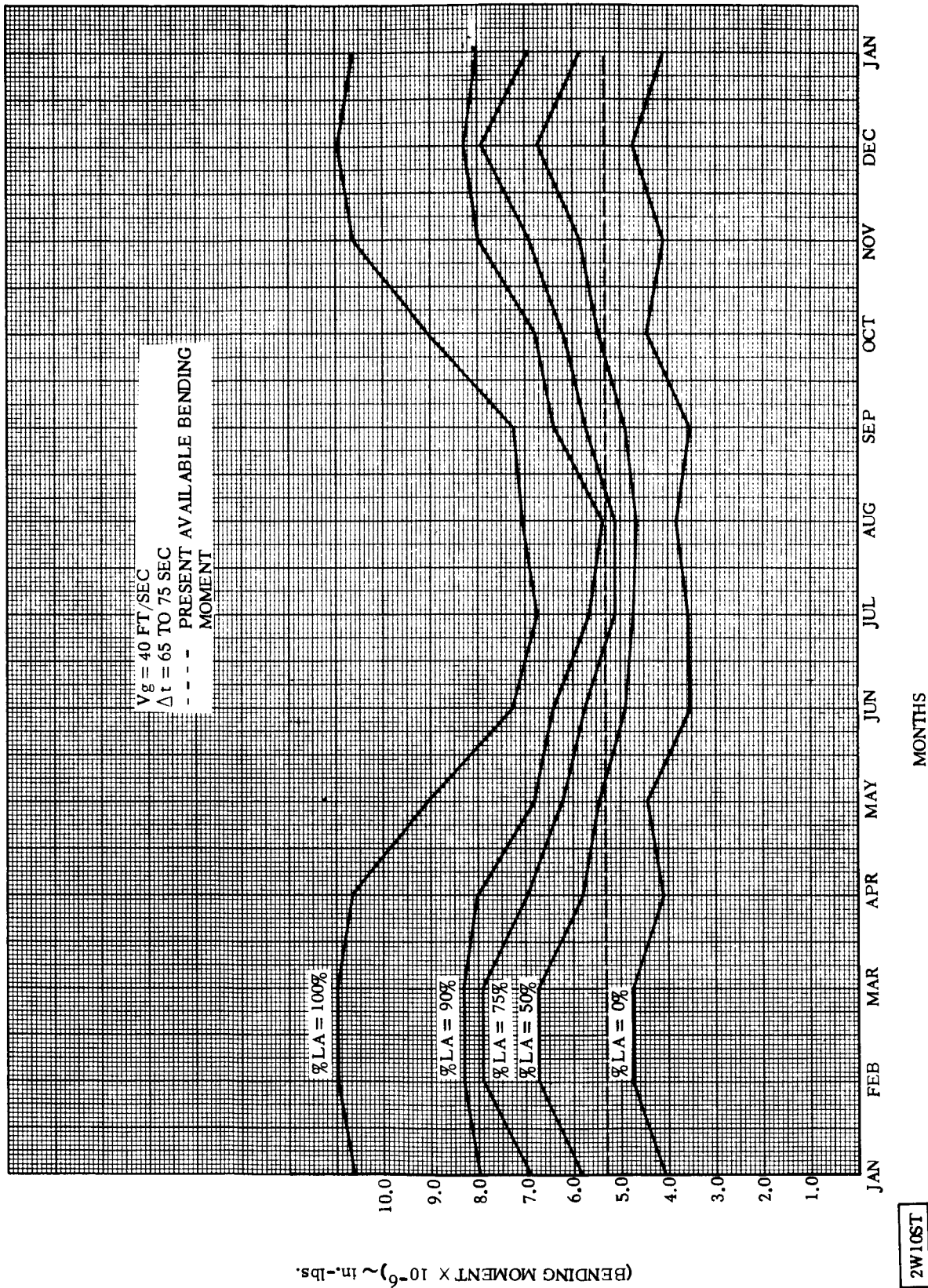


Figure 3-8. Bending Moments Needed for Specific Launch Availability Versus Months for Station 770 (40 ft/sec)

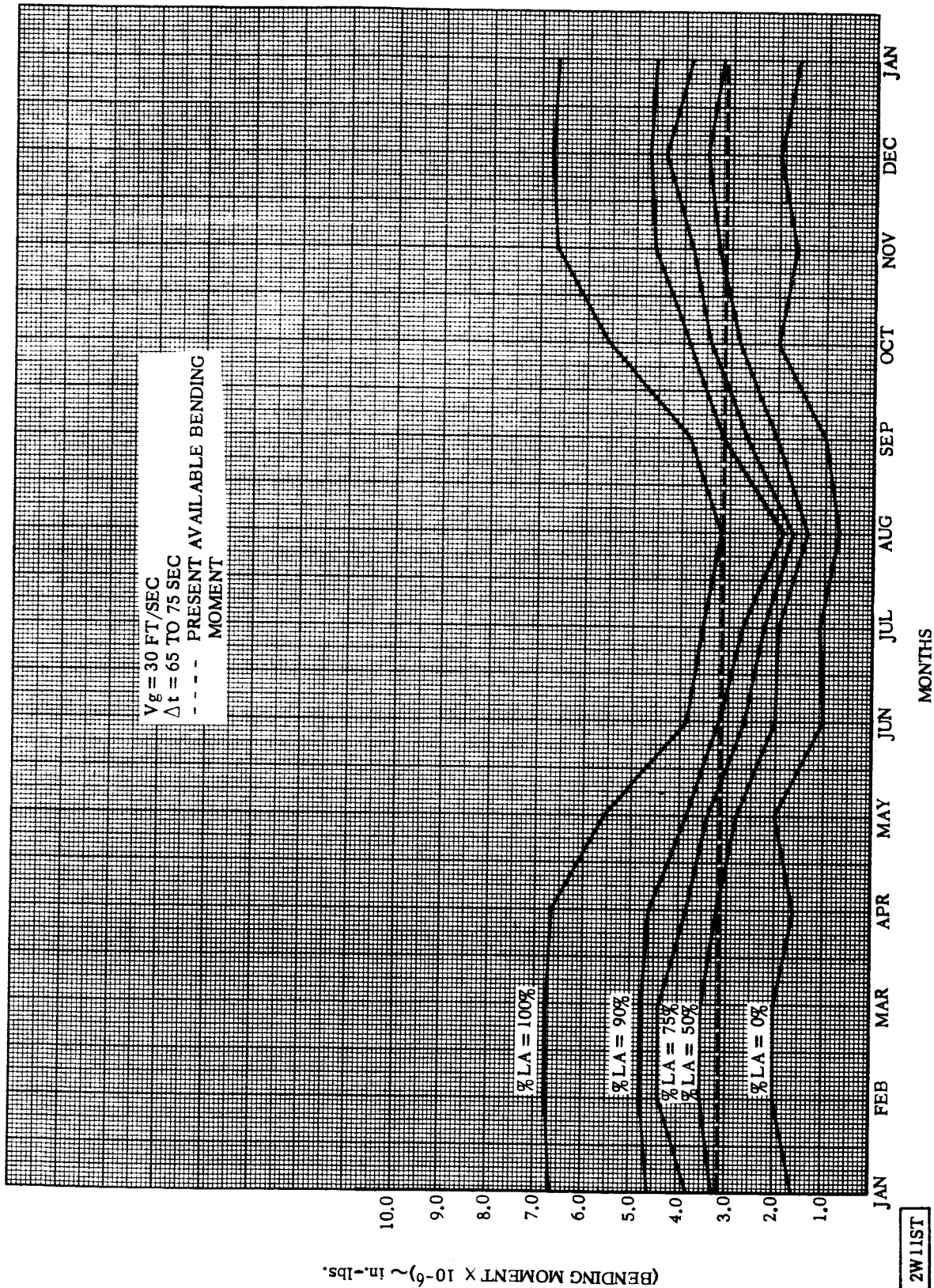


Figure 3-9. Bending Moments Needed for Specific Launch Availability Versus Months for Station 410 (30 ft/sec)

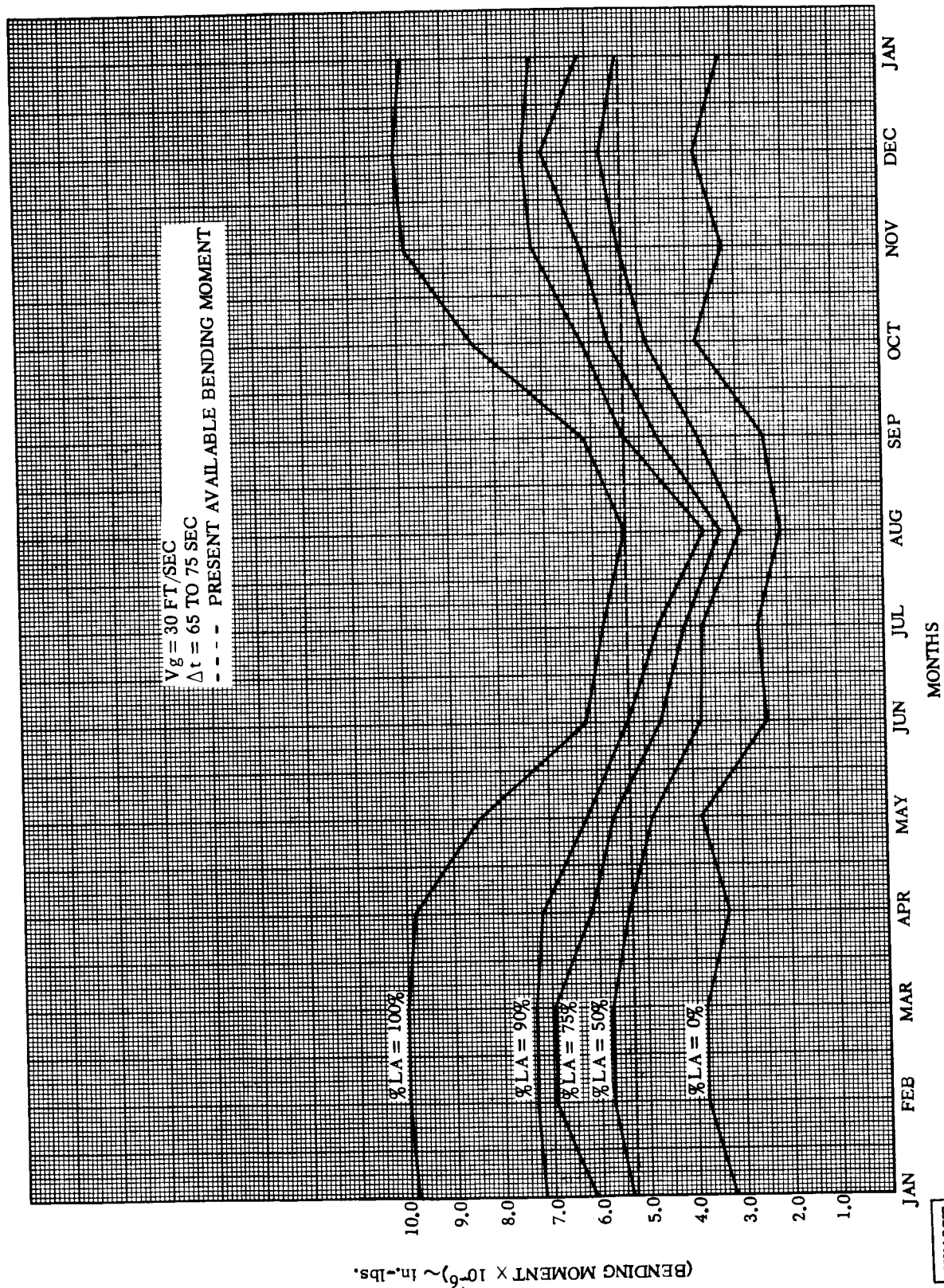


Figure 3-10. Bending Moments Needed for Specific Launch Availability Versus Months for Station 770 (30 ft/sec)

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When βq is large the bending moment needed for a particular percent launch availability in the range of $90\% \leq \% \text{L.A.} \leq 100\%$ is also large. Since the sample size was 30 which is relatively small the maximum βq 's found are not as large as they would be with a large sample, therefore, the bending moments needed for $\% \text{L.A.} = 100\%$ are probably larger than the values found in Figures 3-7 to 3-10. It is felt that the bending moments needed for $0\% \leq \% \text{L.A.} \leq 90\%$ in Figures 3-7 to 3-10 are accurate under the assumptions that were made in the analysis.

3.2 INFORMATION FOR IMPROVED PITCH PROGRAMS AND NEW YAW PROGRAMS

An ideal pitch program generates an approximately zero angle-of-attack at any time in flight. By observing the SC 4020 plots, Atlas/Centaur (AC-7) Pitch Program Investigation, it was found that the angle-of-attack average for many winds at a given time was not approximately zero so it was decided that improved pitch programs and new yaw programs are needed.

3.2.1 AVERAGE INCREMENTAL ANGLE-OF-ATTACK ($\Delta\alpha$ AND $\Delta\beta$). The values of ($\Delta\alpha$) in the alpha plane and the values of ($\Delta\beta$) in the beta plane were found for 10 second increments in the range of $40 \text{ seconds} \leq t \leq 90 \text{ seconds}$. Referring to Figure A-5 in the Appendix for $\Delta t = 50$ to 60 seconds or $t = 55$ seconds it was found that the angle-of-attack is equal to $-.8$ degrees, therefore, the angle-of-attack should be biased by an incremental $\Delta\alpha = +.8$ degrees to give zero angle-of-attack in this case. After checking 30 SC 4020 plots for September wind profiles it was found that the average $\Delta\alpha = -.1$ degrees. The current no wind bias = $.3$ degrees and subtracting $.1$ degrees from this value the best no wind bias = $+.2$ degrees for September. Using the same procedure as shown above for the best three pitch programs Table 3-1 to 3-3 were obtained. Figure 3-11 shows a plot of the average incremental angle-of-attack versus time in flight for the alpha and beta planes. By using these values of the average incremental angle-of-attack better pitch and new yaw programs can be generated.

3.2.2 CONCLUSIONS. The information from Figure 3-11 has been sent to the Centaur Aeroballistics Group. After they develop new pitch and yaw programs, the results will be returned to the Centaur Dynamics Group. From this point, the information will be used to obtain new Atlas/Centaur (AC-7) Pitch Program Investigation Plots. These plots will then be checked to determine how much the percent launch availability will be increased.

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TABLE 3-7. CURRENT NO WIND BIAS, AVERAGE INCREMENTAL ANGLE ANGLE OF ATTACK, AND BEST NO WIND BIAS FOR PP 130

| Time (sec) $\Delta \alpha$ | Current No Wind Bias | Average Incremental Angle of Attack ($\Delta \alpha$) | Best No Wind Bias |
|----------------------------|----------------------|---|-------------------|
| 45 | +1.3 | +1.1 | +2.4 |
| 55 | +1.7 | + .4 | +2.1 |
| 65 | +1.4 | + .2 | +1.6 |
| 75 | + .6 | + .1 | + .7 |
| 85 | - .5 | + .4 | - .1 |
| Time (sec) $\Delta \beta$ | Current No Wind Bias | Average Incremental Angle of Attack ($\Delta \beta$) | Best No Wind Bias |
| 45 | 0 | -1.7 | -1.7 |
| 55 | 0 | -1.6 | -1.6 |
| 65 | 0 | -1.3 | -1.3 |
| 75 | - .1 | - .6 | - .7 |
| 85 | - .1 | + .2 | + .1 |

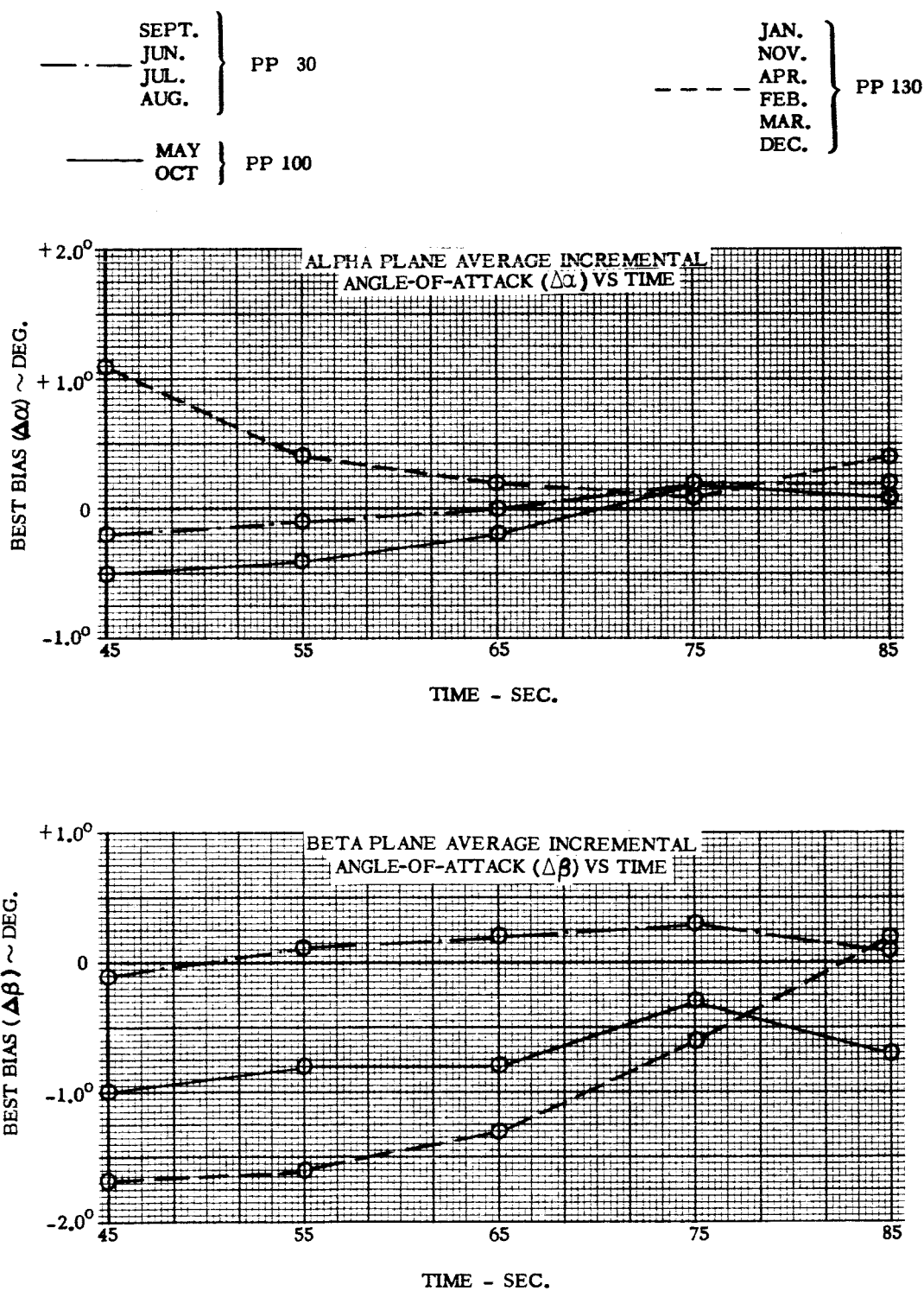
TABLE 3-8. CURRENT NO WIND BIAS, AVERAGE INCREMENTAL ANGLE ANGLE OF ATTACK, AND BEST NO WIND BIAS FOR PP 100

| Time (sec) $\Delta \alpha$ | Current No Wind Bias | Average Incremental Angle of Attack ($\Delta \alpha$) | Best No Wind Bias |
|----------------------------|----------------------|---|-------------------|
| 45 | +1.3 | - .5 | + .8 |
| 55 | +1.2 | - .4 | + .8 |
| 65 | +1.0 | - .2 | + .8 |
| 75 | + .3 | + .2 | + .5 |
| 85 | - .7 | + .1 | - .6 |
| Time (sec) $\Delta \beta$ | Current No Wind Bias | Average Incremental Angle of Attack ($\Delta \beta$) | Best No Wind Bias |
| 45 | 0 | -1.0 | -1.0 |
| 55 | 0 | - .8 | - .8 |
| 65 | 0 | - .8 | - .8 |
| 75 | - .1 | - .3 | - .4 |
| 85 | - .1 | - .7 | - .8 |

TABLE 3-9. CURRENT NO WIND BIAS, AVERAGE INCREMENTAL ANGLE ANGLE OF ATTACK, AND BEST NO WIND BIAS FOR PP 30

| Time (sec) $\Delta \alpha$ | Current No Wind Bias | Average Incremental Angle of Attack ($\Delta \alpha$) | Best No Wind Bias |
|----------------------------|----------------------|---|-------------------|
| 45 | + .4 | - .2 | + .2 |
| 55 | + .3 | - .1 | + .2 |
| 65 | + .3 | 0 | + .3 |
| 75 | - .1 | + .2 | + .1 |
| 85 | - .5 | + .2 | - .3 |
| Time (sec) $\Delta \beta$ | Current No Wind Bias | Average Incremental Angle of Attack ($\Delta \beta$) | Best No Wind Bias |
| 45 | + .1 | - .1 | 0 |
| 55 | 0 | + .1 | + .1 |
| 65 | 0 | + .2 | + .2 |
| 75 | - .1 | + .3 | + .2 |
| 85 | - .1 | + .1 | 0 |

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Figure 3-11. Average Incremental Angle-of-Attack ($\Delta\alpha$ and $\Delta\beta$) Versus Time

SECTION IV

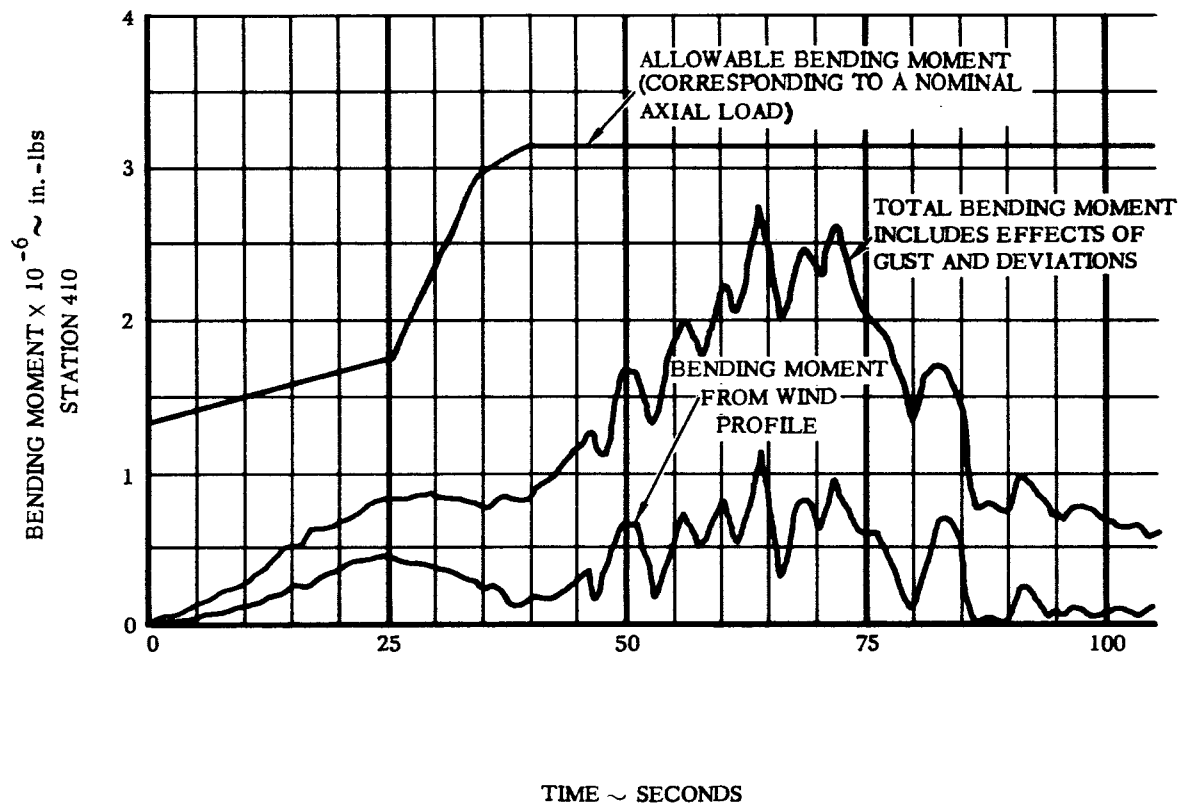
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1. Centaur Monthly Configuration, Performance and Weight Status Report (U) Report No. GD/A63-0495-9, dated 21 February 1964. S.A. Zobal.
2. Monthly and Annual Wind Distribution as a Function of Altitude for Patrick Air Force Base, Cape Kennedy, Florida. Smith, J. W. and Vaughn, W. W. Report No. NASA TN D-610, dated July 1961.
3. Flight Wind Restriction Procedure Atlas/Centaur Flight AC-3. Report No. GD/A BTD 64-070, dated 15 March 1964. J.A. Steele.
4. Atlas/Centaur, AC-5, Static Aeroelastic Factors; GD/A Memo SD-65-10-CEN, 18 January 1965. Author R. Hintz.

APPENDIX A

A-1.1 INTRODUCTION

A-1.1.1 SAMPLE ATLAS/CENTAUR (AC-7) PITCH PROGRAM INVESTIGATION. The following five figures, Figures A-1 through A-5, are a sample of a particular wind profile.



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Figure A-1. Atlas/Centaur (AC-7) Pitch Program Investigation
Bending Moment Station 410 versus Time

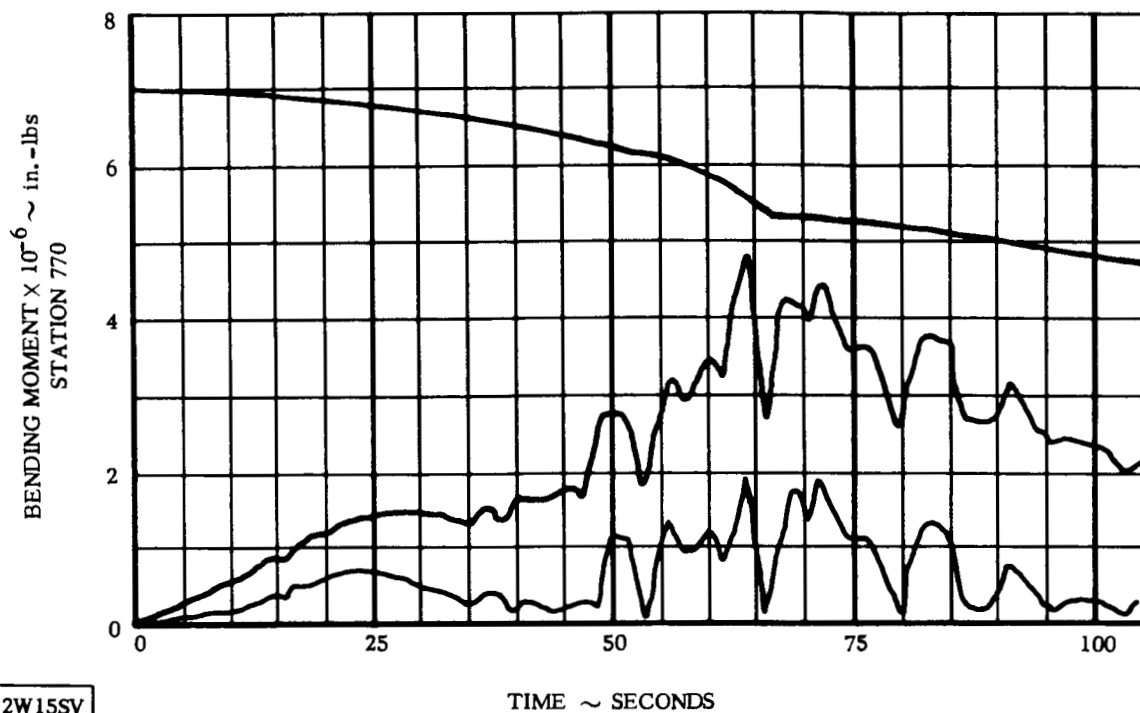


Figure A-2. Atlas/Centaur (AC-7) Pitch Program Investigation
Bending Moment Station 770 versus Time

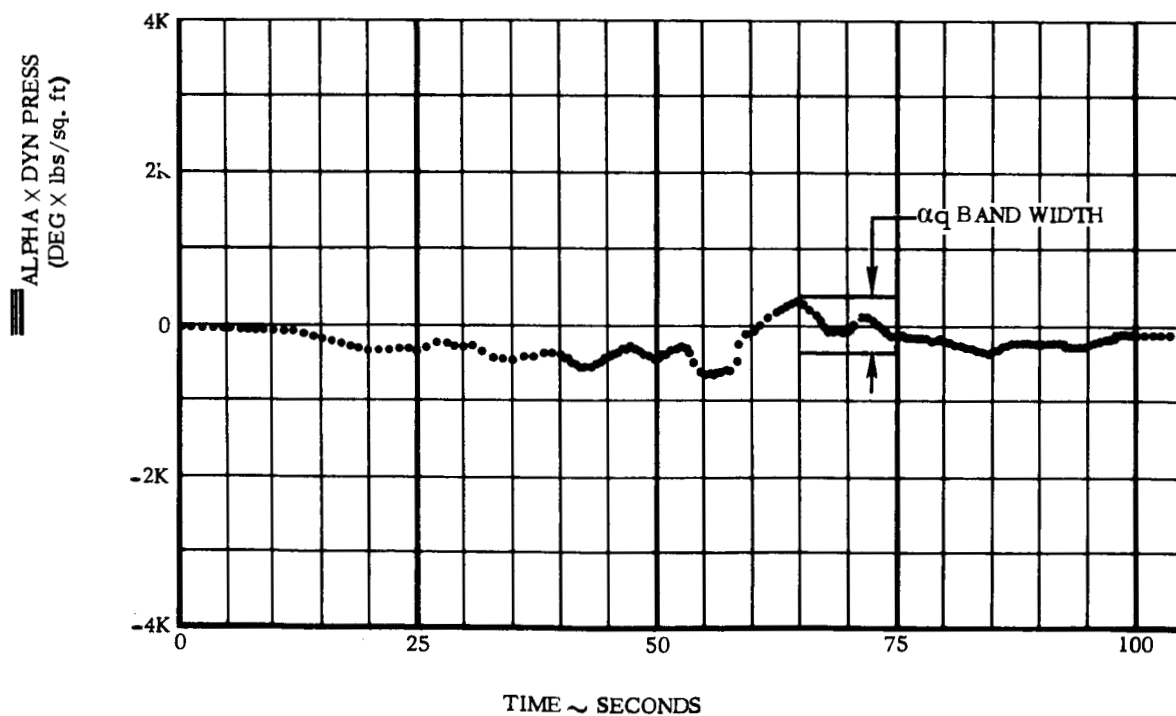
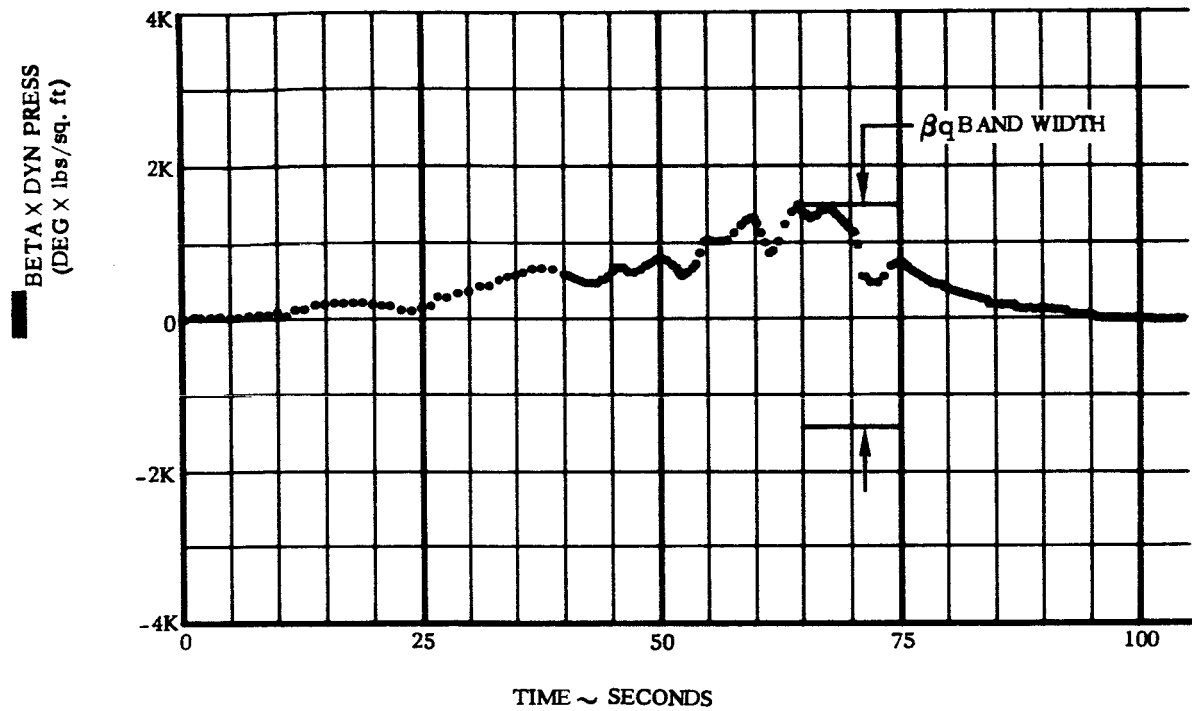
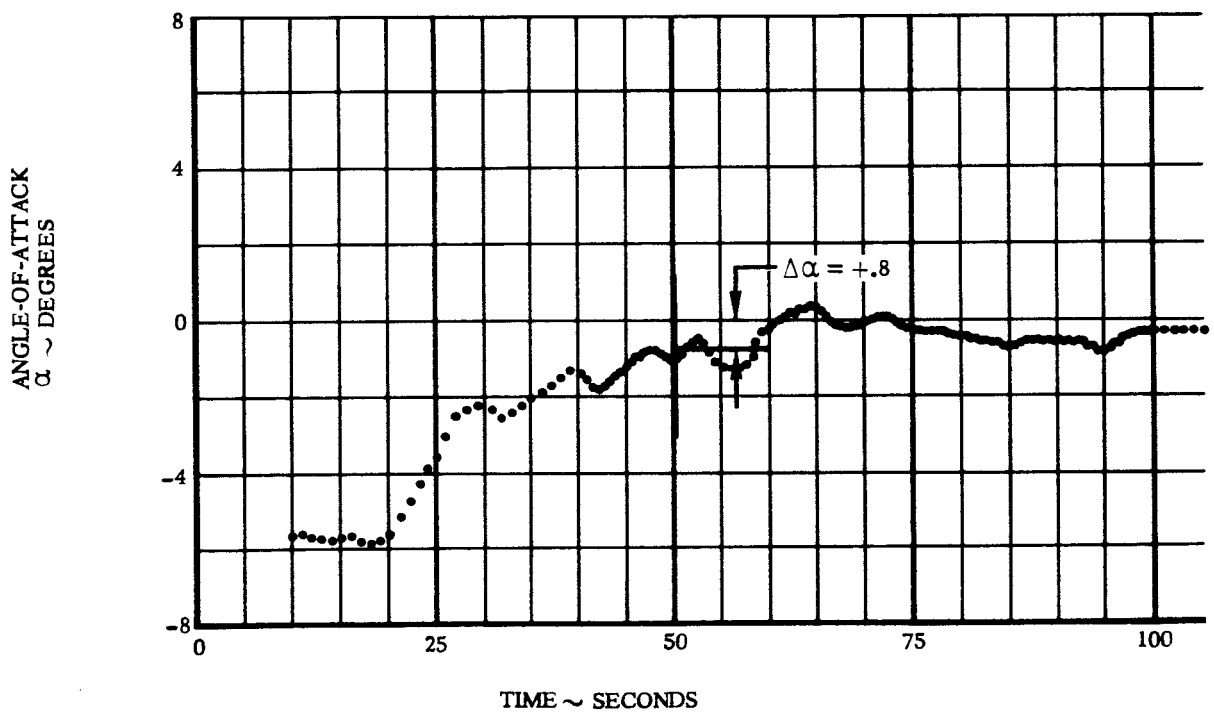


Figure A-3. Atlas/Centaur (AC-7) Pitch Program Investigation
 α_q versus Time



2W17SV

Figure A-4. Atlas/Centaur (AC-7) Pitch Program Investigation
 β_q versus Time



2W18SV

Figure A-5. Atlas/Centaur (AC-7) Pitch Program Investigation
Alpha versus Time